

# **NT06** Nanotube Tutorial

## **Introduction and Theoretical Background**

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# Outline

- Introduction
  - **Nanocarbon pioneers**
  - **What is so special about carbon nanotubes?**
- Theoretical tools
  - **Computational tools**
  - **State of the art of computer simulations**
- Morphology
  - **Relationship to graphite**
  - **Classification of nanotubes**
  - **Structure of nanocarbons and Euler's Theorem**
  - **Polymorphism due to high-temperature synthesis**
  - **Carbon and non-carbon nanotubes**
- Electronic structure and conductivity
  - **Morphology determines conductivity**
  - **Band structure and density of states**
  - **Ballistic and diffusive conduction**
  - **Beware of contacts!**
- Mechanical properties
  - **Graphitic  $sp^2$  versus diamond  $sp^3$  bonding**
  - **High Young's modulus**
- Chemical and thermal resilience, and thermal conductivity
  - **Chemical resilience**
  - **Thermal stability**
  - **High thermal conductivity**
  - **Thermal contraction**
- Summary and Conclusions

# Introduction

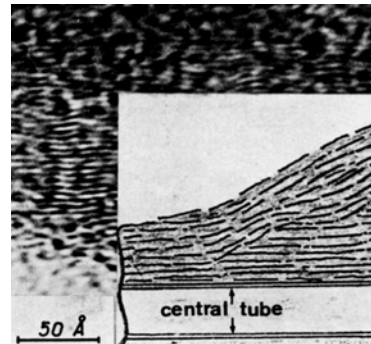
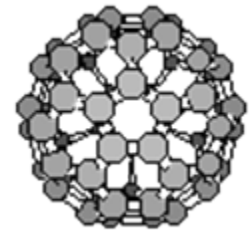
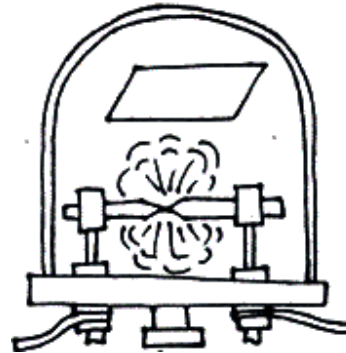
## Nanocarbon pioneers

- The C<sub>60</sub> 'buckyball' and other fullerenes:

- successful synthesis
- potential applications:
  - lubrication
  - superconductivity

- Nanotubes:

- successful synthesis
- potential applications:
  - composites
  - Li-ion batteries
  - medication delivery
  - EMI shielding
  - flat-panel displays
  - super-capacitors
  - fuel cells
  - hydrogen storage

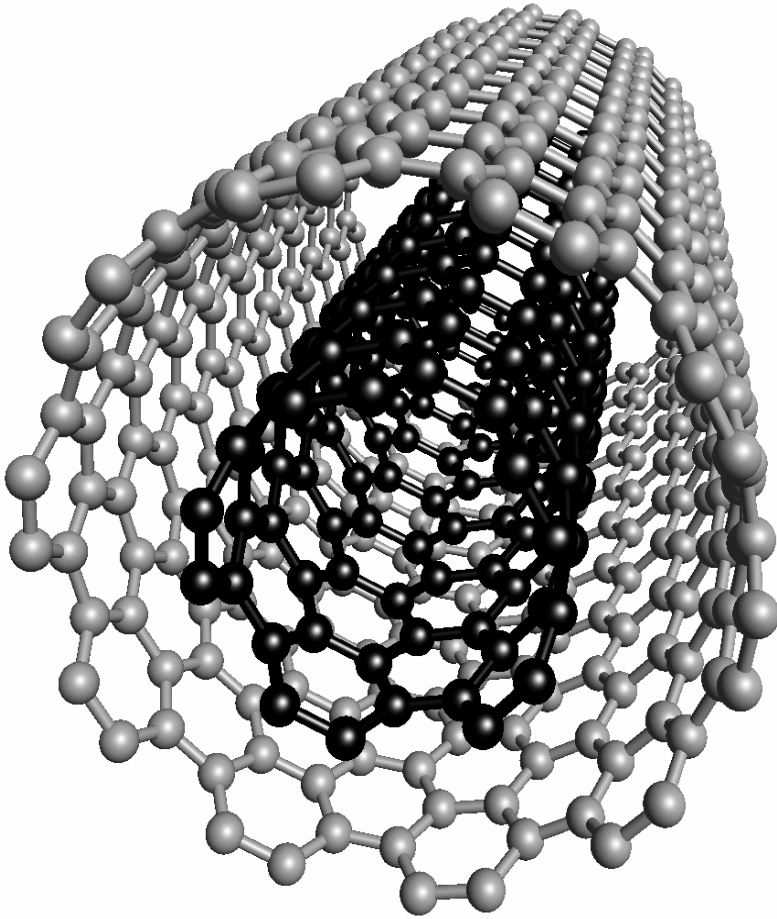


*Nanotubes in the core of carbon fibers:*

A. Oberlin, M. Endo, and T. Koyama, *J. Cryst. Growth* **32**, 335 (1976)

*Nanotubes on the cathode in carbon arc:*  
S. Iijima, *Nature* **354**, 56 (1991)

# What is so special about carbon nanotubes?

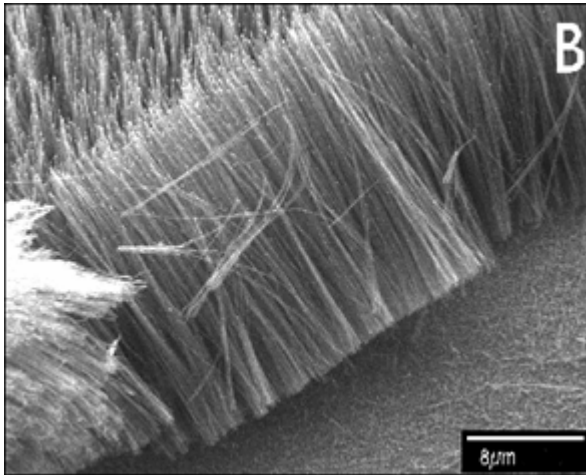


- 1-20 nm diameter
- Atomically perfect
- Chemically inert
- 100 times stronger than steel
- Extremely high melting temperature
- Ideal (ballistic) conductors of electrons, or insulators
- Ideal heat conductors

# Unique properties of nanotubes lead to unique applications

- Sharp and long (<1 cm): large aspect ratio  $1:10^6$  – field emission, electrically conductive composites
- Highest current density  $10^9$  A/cm<sup>2</sup> – Vias, Field Emitters
- Ballistic electron transport – Field Effect Transistors
- Highest Young's modulus, ~1TPa – fibers, composites
- Highest thermal conductivity, 4000 W/(m·K) – composites
- Large electrode potential range/surface area – sensors, supercapacitors

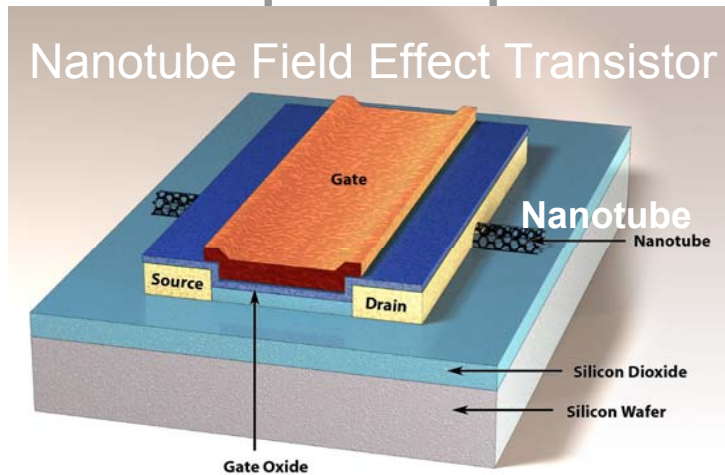
Nanotubes grow by decomposing carbon compounds ...



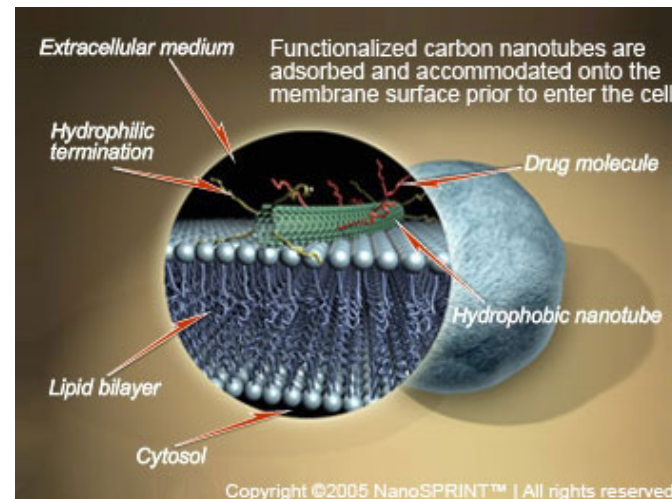
... to make bright flat-panel displays ...



... field-effect transistors for the next generation of computer chips ...



... or deliver drugs



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# Theoretical tools

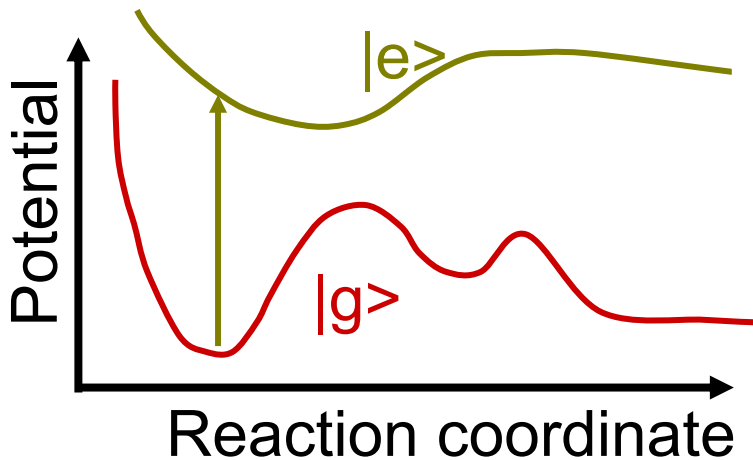
## Computational tools

- **High-end calculations (no adjustable parameters):**
  - Total energy and electronic structure calculations based on the *ab initio* Density Functional formalism
  - Time evolution of electronic wave functions: Time-Dependent Density Functional formalism
  - Optical properties: Self-energy equation yields electron binding energies (GW approximation), Bethe-Salpeter equation also describes excitons
  - Atomic motion: Molecular dynamics simulations with electrons in the ground and excited state
- **Parametrized atomic-scale calculations:**
  - Tersoff-Brenner potential structure and deformation energies
  - Tight-binding formalism for energy and electronic structure
  - Hückel formalism (single-band tight-binding) for basic electronic structure
- **Continuum calculations:**
  - Continuum elasticity theory for deformation energies



# Ground-state versus excited-state calculations

What approach to use?



**Excited state dynamics:**

Solve the time-dependent Schrödinger equation

$$H \psi_n = \epsilon_n \psi_n$$

Density Functional Theory

(codes including SIESTA, VASP, CASTEP, GAUSSIAN, etc.)

**FPSEID** (éf-psai-dí:)

**F**irst-**P**inciples **S**imulation tool for **E**lectron-**I**on **D**ynamics

- Based on time-dependent density functional theory (TDDFT):

*E. Runge and E. K. U. Gross, Phys. Rev. Lett. 52, 997 (1984).*

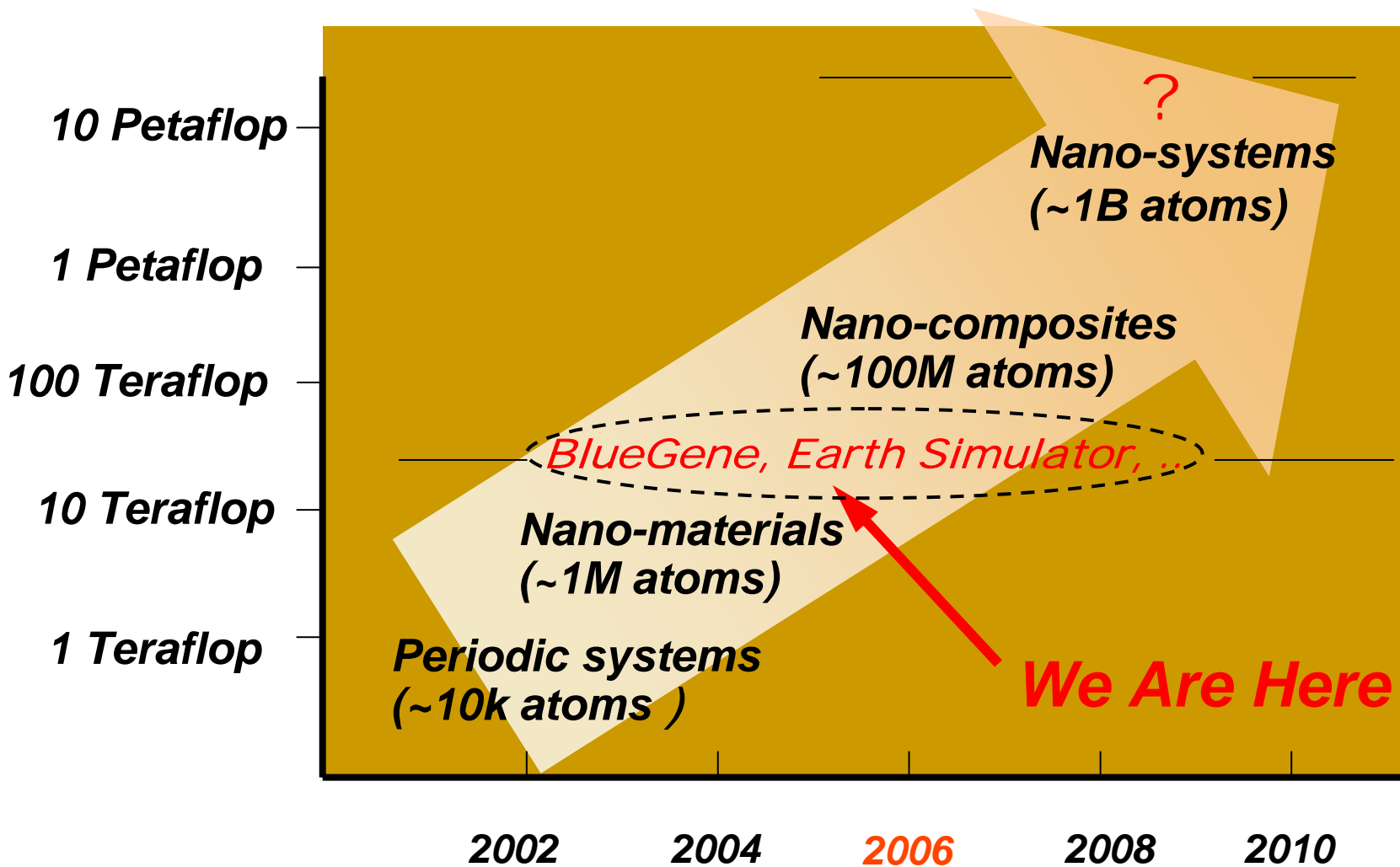
- Computational details for real-time MD simulations:

*Sugino & Miyamoto PRB 59, 2579 (1999) ; ibid, B 66, 89901(E) (2002),*

using the Suzuki-Trotter split operator method to compute the time-propagator

Need massively parallel computer architectures and suitable algorithms distribute load over processors for speed-up

# State of the art computer simulations



# Computational Nanotechnology Laboratory: Earth Simulator, Tokyo

www.nytimes.com

**The New York Times**  
ON THE WEB

April 20, 2002

## Japanese Computer Is World's Fastest, as U.S. Falls Back

By JOHN MARKOFF

**S**AN FRANCISCO, April 19 — A Japanese laboratory has built the world's fastest computer, a machine so powerful that it matches the raw processing power of the 20 fastest American computers combined and far outstrips the previous leader, an L.B.M.-built machine.

**Cost:**  
**\$500,000,000**  
**Maintenance:**  
**\$50,000,000/year**

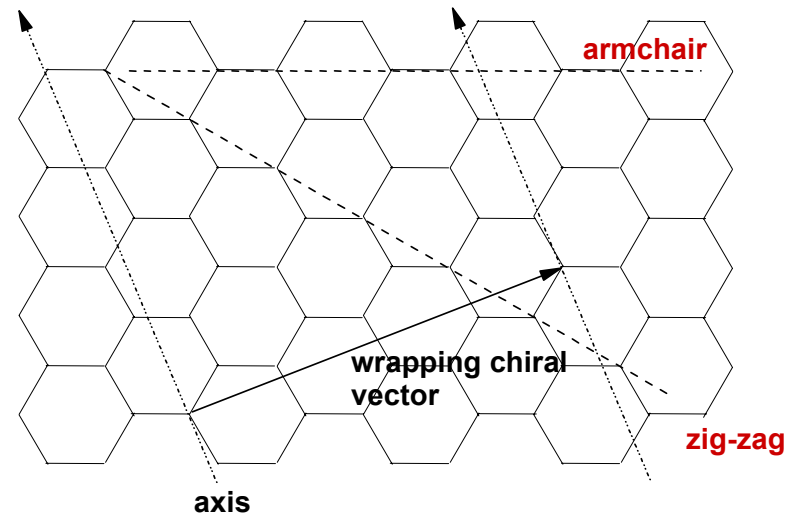
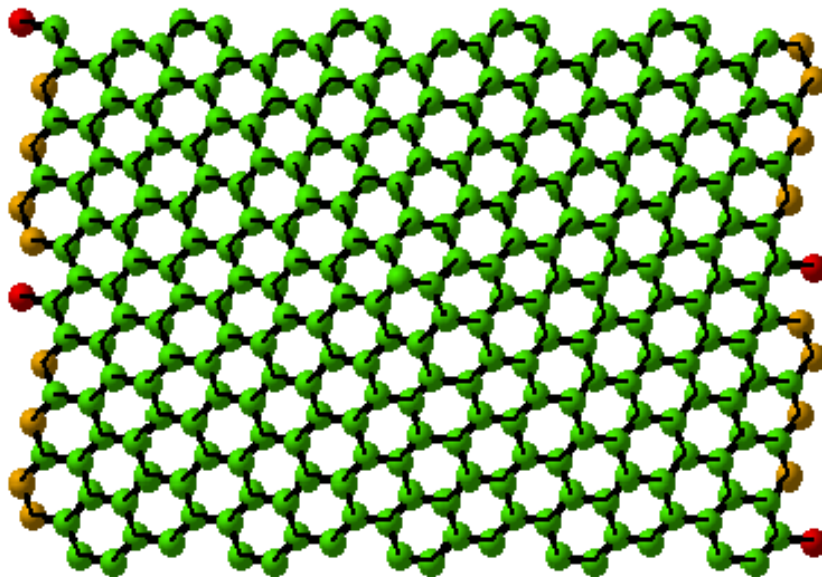
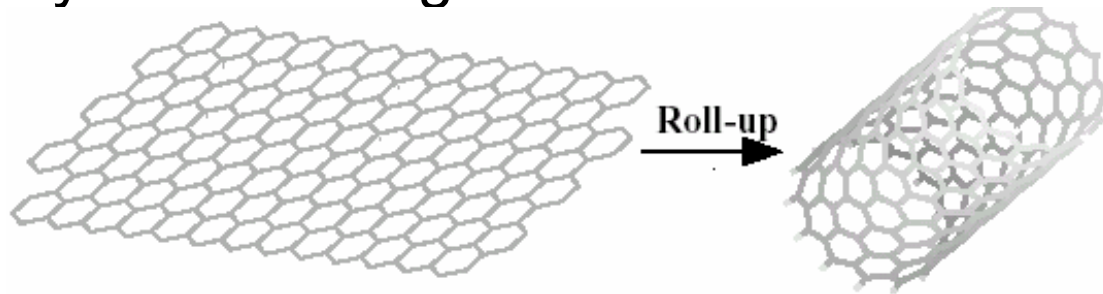
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# Morphology

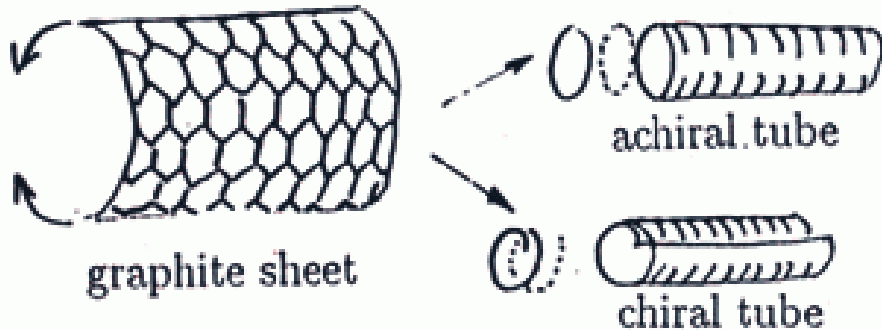
## Relationship to graphite

- A nanotube is formed by rolling up a graphene layer to a contiguous tube

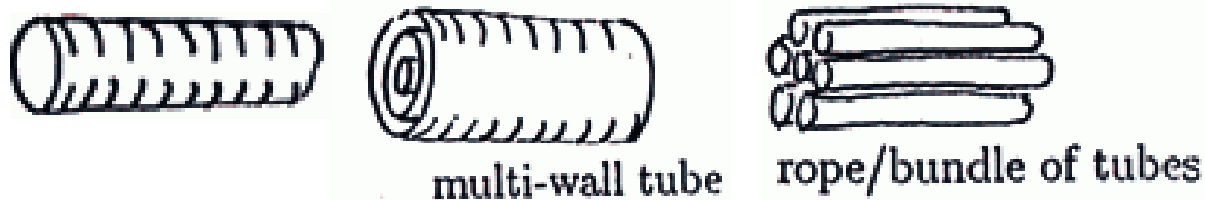


# Classification of nanotubes

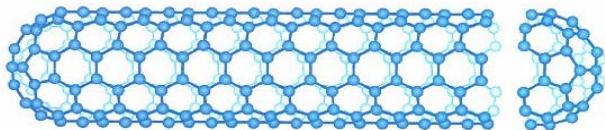
- Achiral and chiral nanotubes



- Single-wall, multi-wall tubes, and ropes



- Open-ended and capped nanotubes



- Zigzag and armchair achiral nanotubes

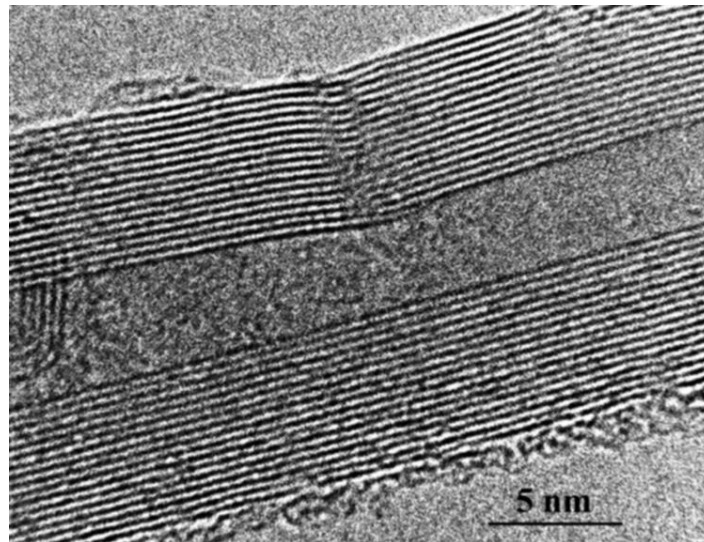
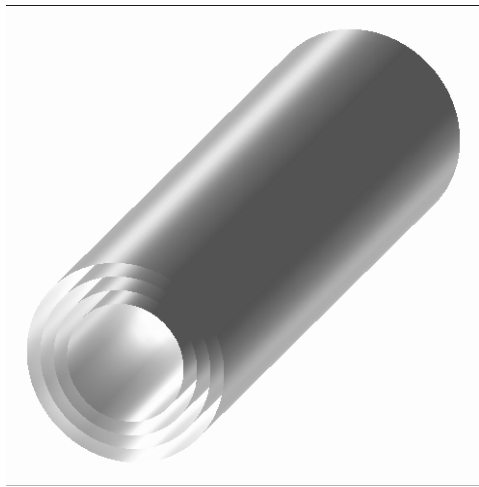


$(n, 0)$ : zig-zag nanotube



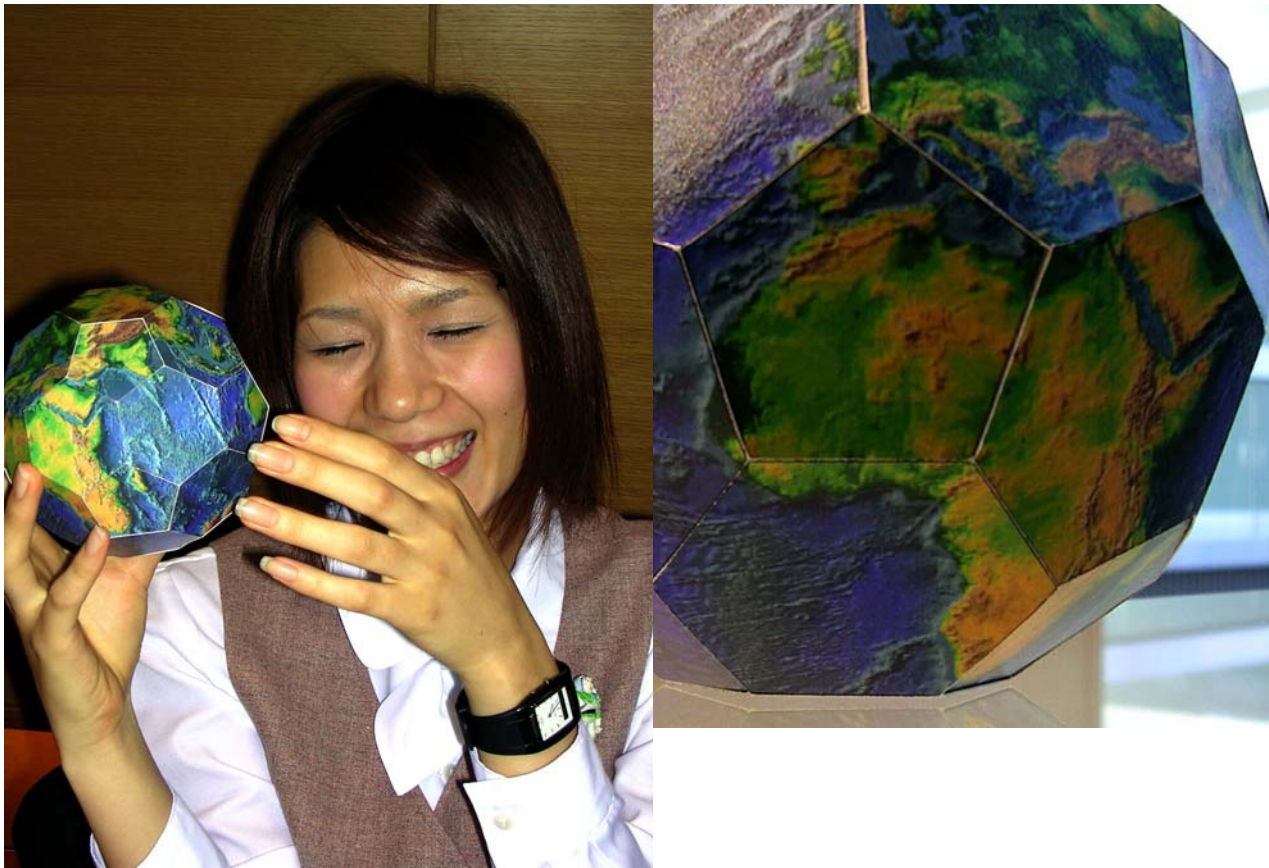
$(n, n)$ : armchair nanotube

- Multi-wall tubes and scrolls



# Structure of nanocarbons and Euler's Theorem

- Example 1: Objects of topological gender 0  
(polyhedra with no holes, e.g.  $C_{60}$  "buckyball")





# Objects of topological gender 0

(polyhedra with no holes, e.g. C<sub>60</sub> buckyball")

- **C – E + F = 2 Euler's Theorem**

- C = number of Corners
- E = number of Edges
- F = number of Faces

- Assume only pentagons, hexagons in the structure

- p = number of pentagons (5 corners)
- x = number of hexagons (6 corners)

- $C = p \cdot 5/3 + x \cdot 6/3$

- $E = p \cdot 5/2 + x \cdot 6/2$

- $F = p + x$

- Substitute C, E, F in Euler's Theorem:

$$(5/3)p + (6/3)x - (5/2)p - (6/2)x + p + x = 2$$

$$(5/3 - 5/2 + 1)p + (6/3 - 6/2 + 1)x = 2$$

$$(1/6)p + 0x = 2$$

$$p/6 = 2$$

**p = 12**    x=arbitrary

# Objects of topological gender 0

(polyhedra with no holes, e.g. C<sub>60</sub> buckyball")

- Assume also heptagons in the structure
  - p = number of pentagons (5 corners)
  - x = number of hexagons (6 corners)
  - h = number of heptagons (7 corners)
  
  - $C = p \cdot 5/3 + x \cdot 6/3 + h \cdot 7/3$
  - $E = p \cdot 5/2 + x \cdot 6/2 + h \cdot 7/2$
  - $F = p + x + h$
  
  - Substitute C, E, F in Euler's Theorem:  
 $C - E + F = 2$  Euler's Theorem  
 $(5/3)p + (6/3)x - (5/2)p - (6/2)x + p + x = 2$   
 $(5/3 - 5/2 + 1)p + (6/3 - 6/2 + 1)x + (7/3 - 7/2 + 1)h = 2$   
 $(1/6)p + 0x - (1/6)h = 2$

$$p - h = 12 \quad x = \text{arbitrary}$$

- **Example 2: Objects of topological gender 1**  
(polyhedra with one hole, e.g. “donut”)

- **$C - E + F = 0$  Euler’s Theorem**

- C = number of Corners
- E = number of Edges
- F = number of Faces

- Assume only pentagons, hexagons in the structure

- p = number of pentagons (5 corners)
- x = number of hexagons (6 corners)

- Substitute C, F, F in Euler’s Theorem:

$$(1/6) p + 0x = 0$$

$$p/6 = 0$$

- no pentagons, only hexagons: perfect cylindrical segment



$$p = 0 \quad x = \text{arbitrary}$$

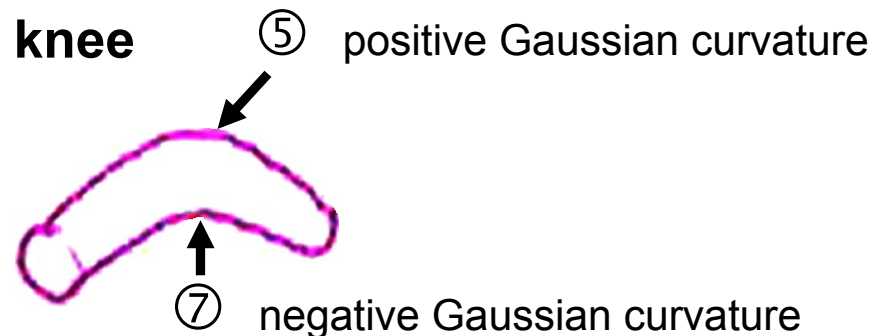
# Objects of topological gender 1

(polyhedra with one hole, e.g. “donut”)

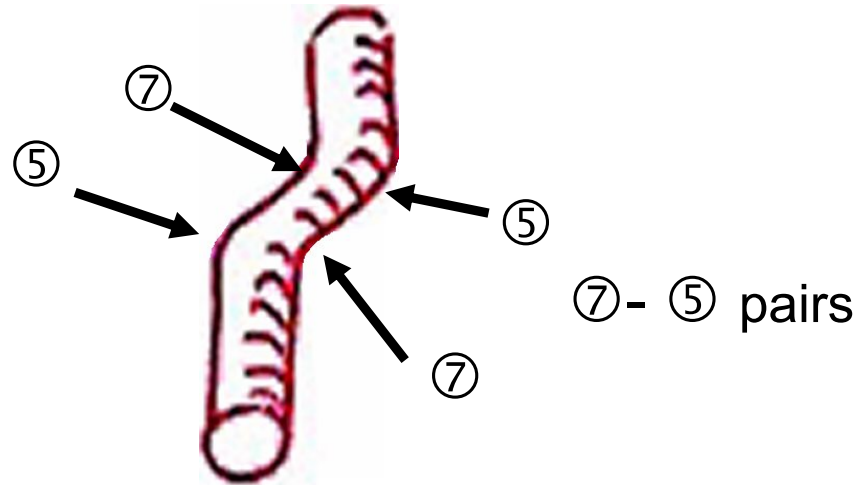
- Assume also heptagons in the structure
  - $p$  = number of pentagons (5 corners)
  - $x$  = number of hexagons (6 corners)
  - $h$  = number of heptagons (7 corners)
- Substitute C, F, F in Euler’s Theorem:  
C – E + F = 0 Euler’s Theorem  
 $(1/6)p + 0x - (1/6)h = 0$

$$p = h \quad x = \text{arbitrary}$$

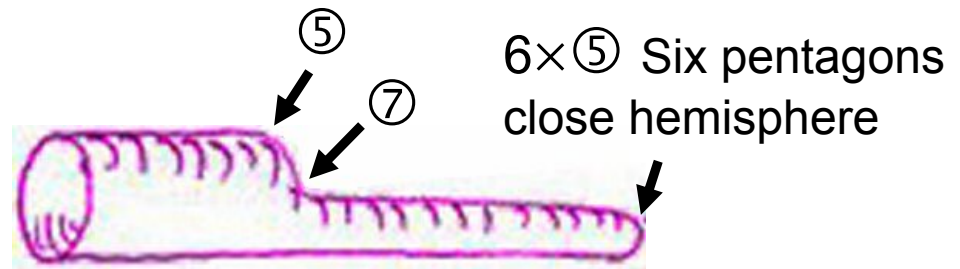
- Illustration 1: **Local curvature at a knee**



- Illustration 2: **Bent tube**



- Illustration 3: **Tube with changing diameter**



# Polymorphism due to high-temperature synthesis

- Production
  - Laser ablation (LA)
  - Carbon Arc (CA)
    - Bottleneck is purification, not raw production
  - Chemical vapor decomposition (CVD)
    - Better for larger scale-up
    - Produces higher purity ('etching')
  - HIPCO
- Synthesis occurs at  $\approx 1000$  K, yielding mixtures of nanotubes
- Applications were critically limited by lack of production – now being fulfilled



# Carbon and non-carbon nanotubes

- Not only  $sp^2$  carbon (graphite), but many **other layered systems form nanotubes**
- Examples: BN,  $BC_3$ ,  $MoS_2$ ,  $MoSe_2$ ,  $WS_2$ ,  $WSe_2$ , ...
- Electronic properties and diameter depend strongly on the system (e.g. ***all*** BN nanotubes are wide-gap semiconductors)

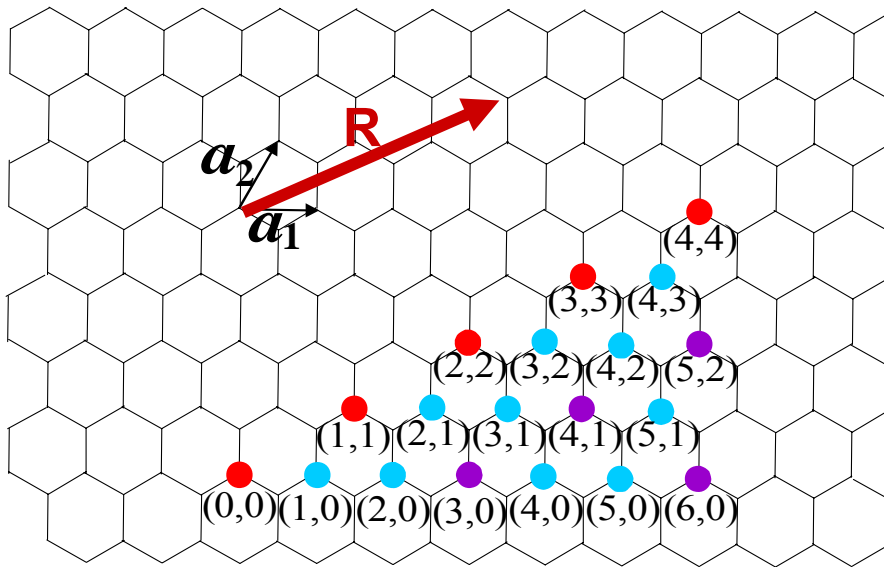
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# Electronic structure and conductivity

## Morphology determines conductivity



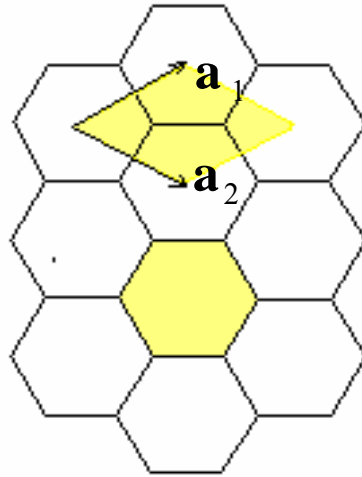
Chiral vector  $\mathbf{R} = n\mathbf{a}_1 + m\mathbf{a}_2$  defines uniquely the  $(n,m)$  nanotube

- *metal*:  $n=m$
- *semimetal*:  $n-m=3p$
- *semiconductor*:  $n-m \neq 3p$  ( $p$  is integer)

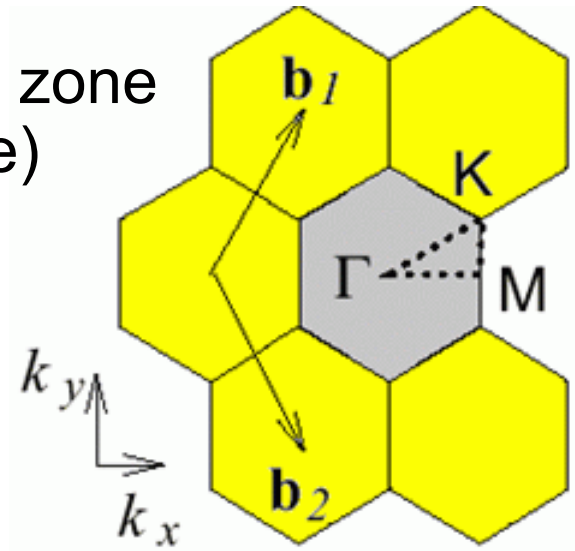
- Large ***variation in conducting behavior*** in all-carbon nanotubes

# Electronic structure of graphite

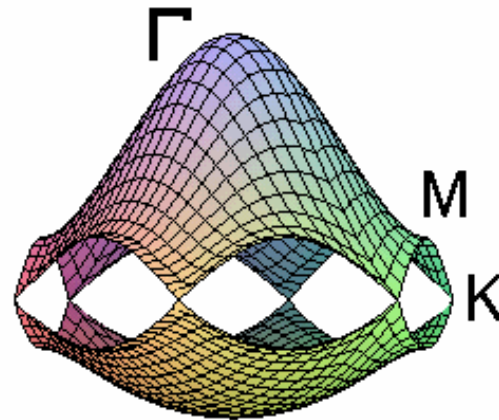
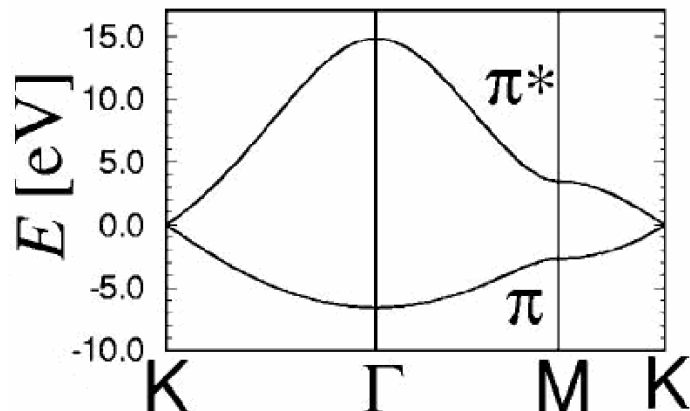
Unit cell  
(real space)



Brillouin zone  
(k-space)

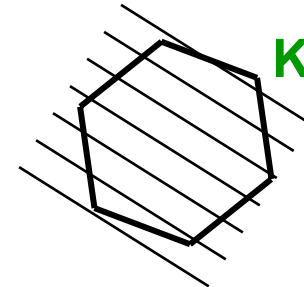
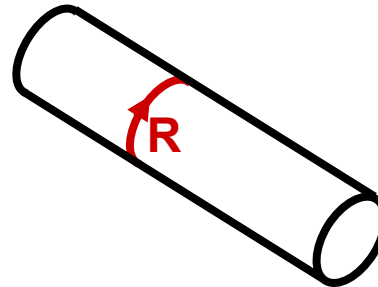
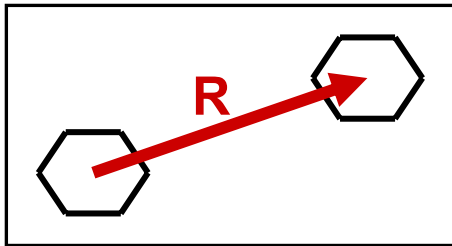


- Dispersion of the graphite  $\pi$  band near  $E_F$ 
  - Graphite is zero-gap semiconductor
  - Fermi point is **K**

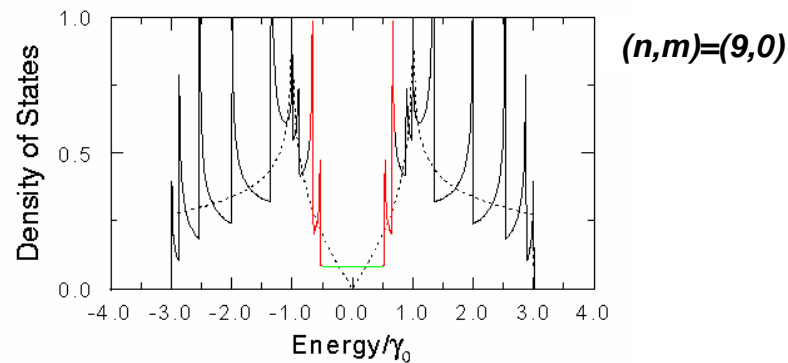
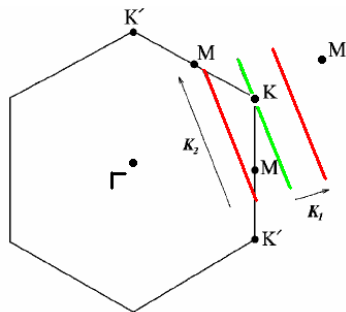


# Metallicity depends on chiral vector

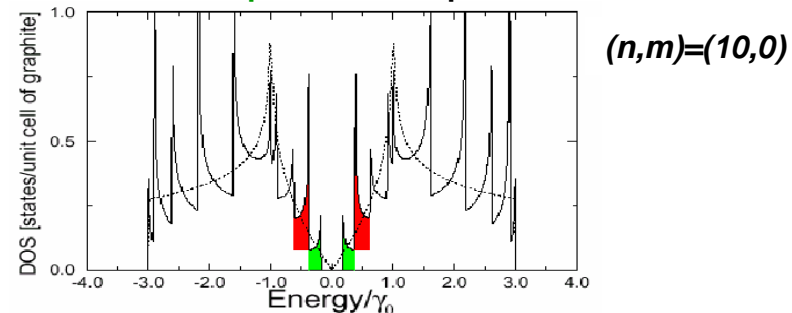
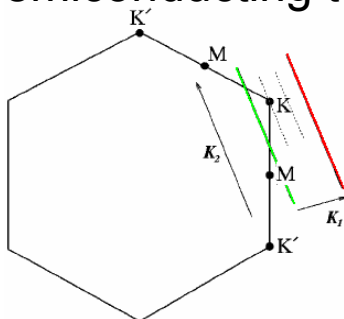
- Electronic structure changes caused by momentum quantization along lines in the Brillouin zone



- Metallic tubes **contain K point** on quantization lines



- Semiconducting tubes **do not contain K point** on quantization lines



Bravais lattice points:  $\mathbf{r} = \mathbf{R} = n\mathbf{a}_1 + m\mathbf{a}_2$   
 $\psi(\mathbf{r}) = e^{i\mathbf{k}\cdot\mathbf{r}} = e^{i\varphi}$  Bloch theorem

Basis points:  $\mathbf{r}' = \mathbf{R} + \boldsymbol{\tau} = (n + \frac{1}{3})\mathbf{a}_1 + (m + \frac{1}{3})\mathbf{a}_2$   
 $\psi(\mathbf{r}') = e^{i\mathbf{k}\cdot\mathbf{r}'} = e^{i\varphi'}$

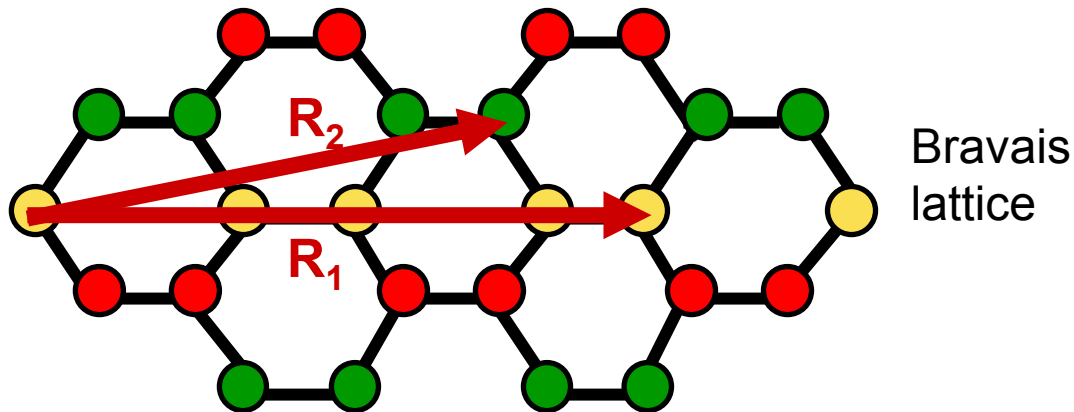
Consider carrier with momentum  $\mathbf{K}$ :

$$\varphi = \mathbf{K}\cdot\mathbf{r} = \frac{1}{3}(\mathbf{b}_2 - \mathbf{b}_1)\cdot(n\mathbf{a}_1 + m\mathbf{a}_2) = \frac{1}{3}(-2\pi n + 2\pi m) = \frac{2\pi}{3}(m - n)$$

$$\varphi' = \mathbf{K}\cdot\mathbf{r}' = \frac{1}{3}(\mathbf{b}_2 - \mathbf{b}_1)\cdot[(n + \frac{1}{3})\mathbf{a}_1 + (m + \frac{1}{3})\mathbf{a}_2] = \frac{1}{3}[-2\pi(n + \frac{1}{3}) + 2\pi(m + \frac{1}{3})] = \frac{2\pi}{3}(m - n)$$

Possible phases:  $0^\circ, +120^\circ, -120^\circ$

Bravais lattice point and basis point have same phase



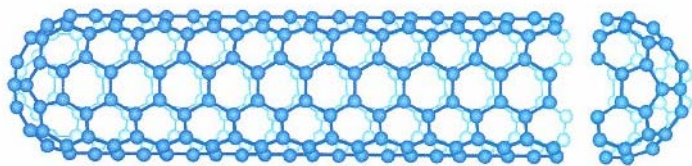
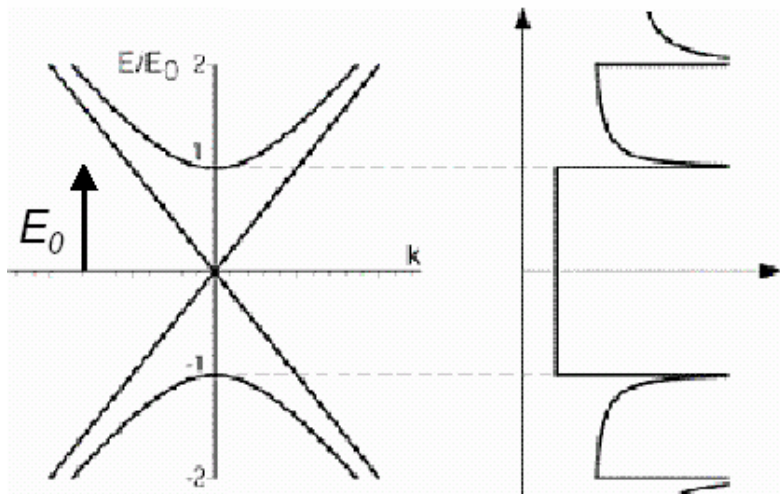
$\mathbf{R}_1$  yields conducting nanotube:  $\mathbf{K}$  is allowed eigenstate

$\mathbf{R}_2$  yields insulating nanotube:  $\mathbf{K}$  is not an allowed eigenstate  
 (i.e. electrons with Fermi momentum are not allowed)

# Band structure and density of states

Type I. Metallic tubes

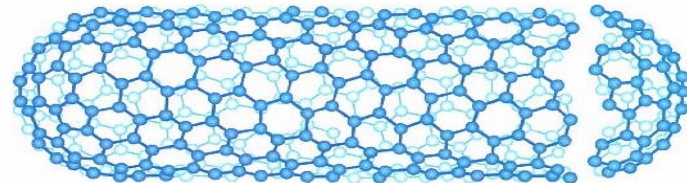
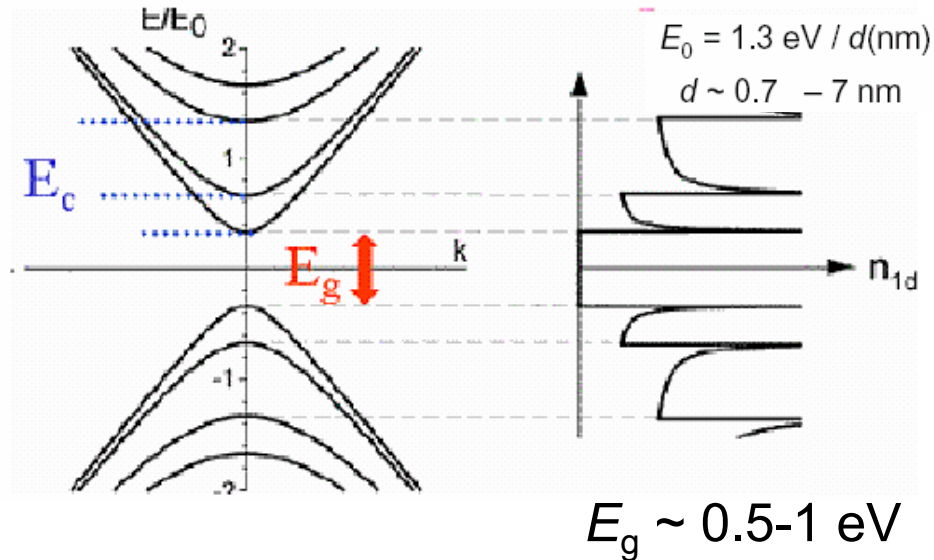
$$M-N = 0 \quad E_g = 0$$



$$(m,n) = (5,5)$$

Type II. Wide-gap semiconducting tubes

$$M-N > 3p \quad E_g = 2/3 E_0$$

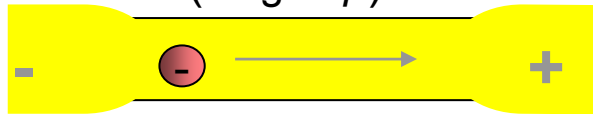


$$(m,n) = (10,5)$$

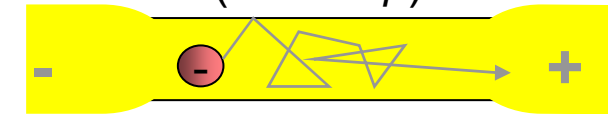
In reality, also Type III: Small-gap semiconducting tubes (zigzag metals)

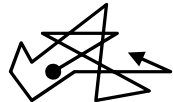

# Ballistic and diffusive conduction

- Carbon nanotubes exhibit **ballistic** or **diffusive** transport

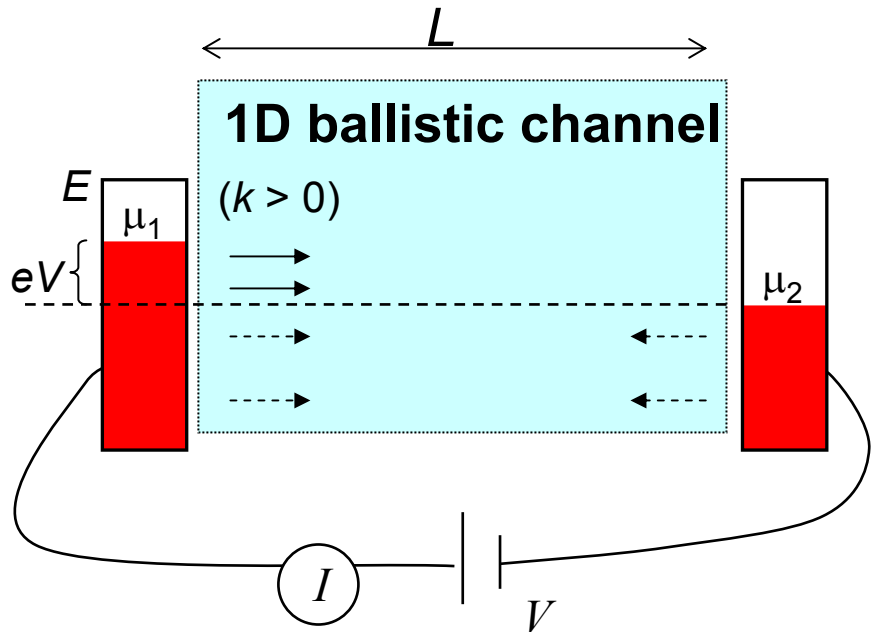


$mfp$ : electron mean free path



- Ballistic transport**,  $L \ll L_m, L_\phi$ 
  - no scattering, only geometry (eg. QPC)
  - when  $\lambda_F \sim L$ : quantized conductance  $G \sim e^2/h$
- Diffusive**,  $L > L_m$ 
  - scattering, reduced transmission
- Localization**,  $L_m \ll L_\phi \ll L$ 
  - $R \sim \exp(L)$  due to quantum interference at low  $T$
- Classical (incoherent)**,  $L_\phi, L_m \ll L$ 
  - ohmic resistors  $T$

- Length Scales:**
  - $\lambda_F$  Fermi wavelength (only electrons close to Fermi level contribute)
  - $L_m$  momentum relaxation length (static scatterers)
  - $L_\phi$  phase relaxation length (fluctuating scatterers)
  - $L$  sample length

# Ballistic conductance in nanowires is quantized



- Contacts: 'Ideal reservoirs'
- Chemical potential  $\mu \sim E_F$  (Fermi level)
- Channel: 1D, ballistic (transport without scattering)

- 1D density of states per unit length:

$$g_{1D}(E) = \frac{2}{h} \sqrt{\frac{2m}{E}} = \frac{2}{hv(E)}$$

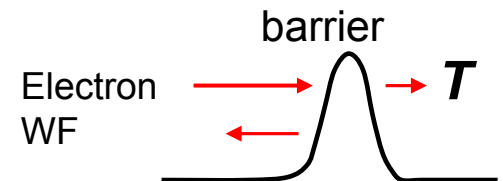
$$I = \int_{\mu_1}^{\mu_2} \underset{\text{velocity}}{ev(E)} \left( \underset{\text{spin}}{2} \underset{k > 0}{\frac{1}{2} g_{1D}(E)} \right) dE = \int_{\mu_1}^{\mu_2} ev(E) \left( \frac{2}{hv(E)} \right) dE = \frac{2e}{h} (\mu_2 - \mu_1) = \frac{2e}{h} (eV)$$

$$G = I/V = \frac{2e^2}{h}$$

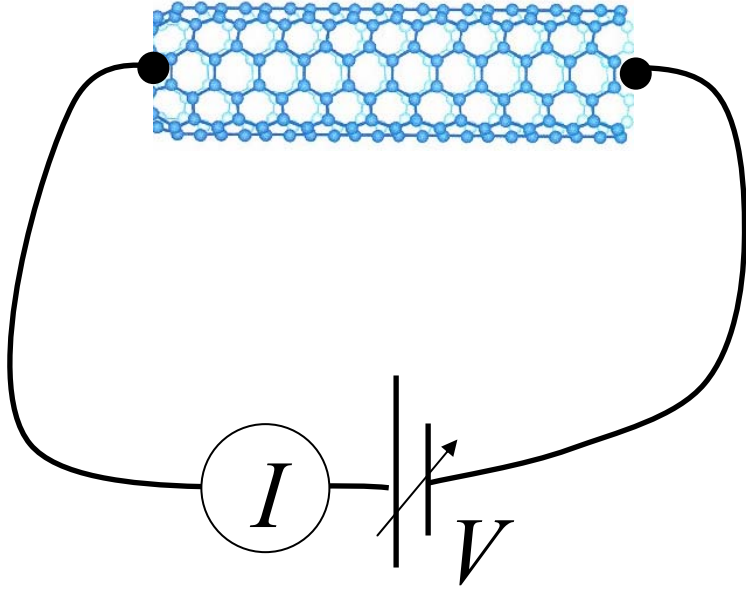
Conductance is fixed, regardless of length  $L$ ;  
(no well defined conductivity  $\sigma$ )

$$G(E_F) = \frac{2e^2}{h} \sum_n T_n(E_F)$$

Landauer formula for  $N$  transmission channels



# Ballistic conductance of a metallic single-wall nanotube



With perfect contacts:

$$G = \text{current} / \text{voltage}$$
$$= 2 * 2e^2 / h$$

(two subbands in NT)

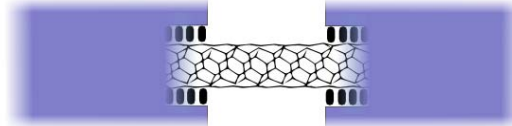
*Quantum of resistance:*  
 $h/e^2 = 25 \text{ k}\Omega$



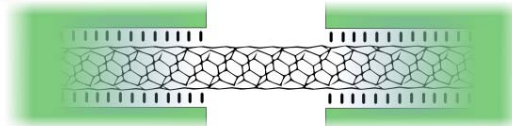
# Beware of contacts!

- Which metal-nanotube contacts optimize charge injection?

- Short, strong contact?

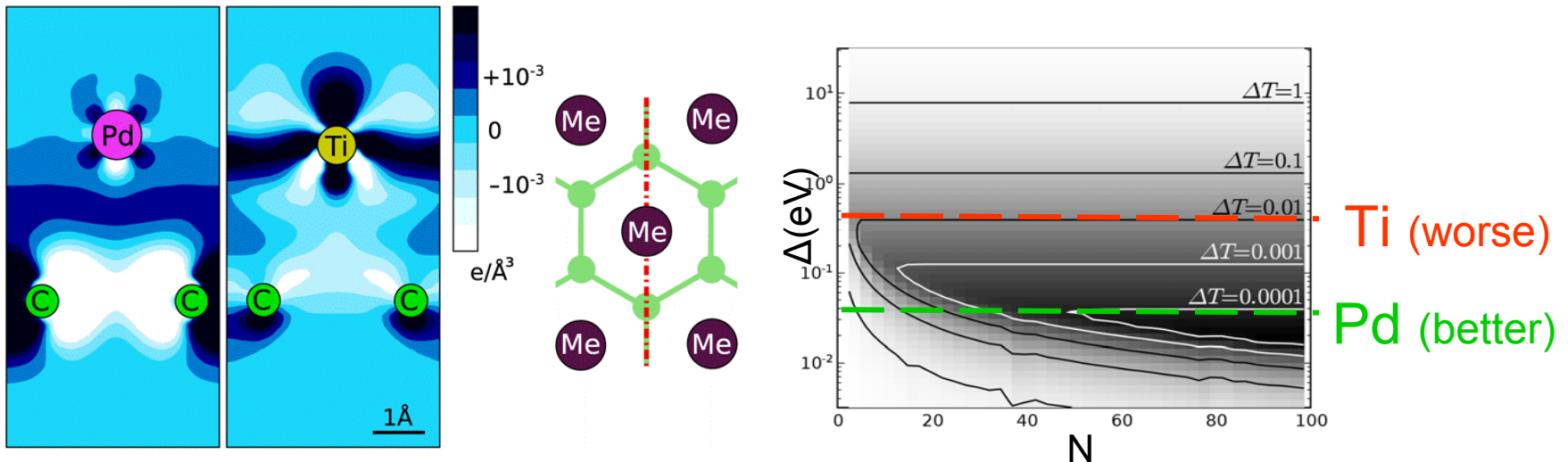


- Long, weak contact?



*N. Nemeč, D. Tomanek,  
G. Cuniberti,  
Phys. Rev. Lett.  
96, 076802 (2006)*

- Charge injection at the Pd/nanotube and Ti/nanotube interface:



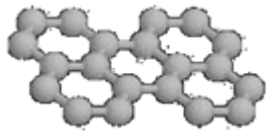
# Outline

- Introduction
  - Nanocarbon pioneers
  - What is so special about carbon nanotubes?
- Theoretical tools
  - Computational tools
  - State of the art of computer simulations
- Morphology
  - Relationship to graphite
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  - Structure of nanocarbons and Euler's Theorem
  - Polymorphism due to high-temperature synthesis
  - Carbon and non-carbon nanotubes
- Electronic structure and conductivity
  - Morphology determines conductivity
  - Band structure and density of states
  - Ballistic and diffusive conduction
  - Beware of contacts!
- **Mechanical properties**
  - **Graphitic  $sp^2$  versus diamond  $sp^3$  bonding**
  - **High Young's modulus**
- Chemical and thermal resilience, and thermal conductivity
  - Chemical resilience
  - Thermal stability
  - High thermal conductivity
  - Thermal contraction
- Summary and Conclusions

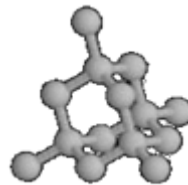
# Mechanical properties

## Graphitic $sp^2$ versus diamond $sp^3$ bonding

- Graphitic  $sp^2$  bonded structures are stiffer than  $sp^3$  bonded diamond



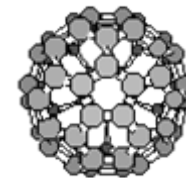
$sp^2$



$sp^3$

$$\frac{\text{Binding Energy}}{3} > \frac{\text{Binding Energy}}{4}$$

$$sp^2 > sp^3$$



# High Young's modulus

- **Prediction:**

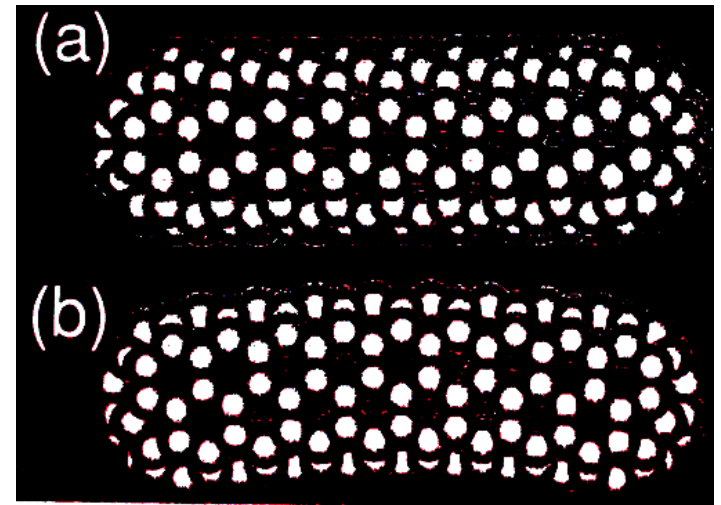
*[G. Overney, W. Zhong, and D. Tomanek: Structural Rigidity and Low Frequency Vibrational Modes of Long Carbon Tubules, Z. Phys. D 27, 93-96 (1993)]*

**$Y \approx 5$  TPa**

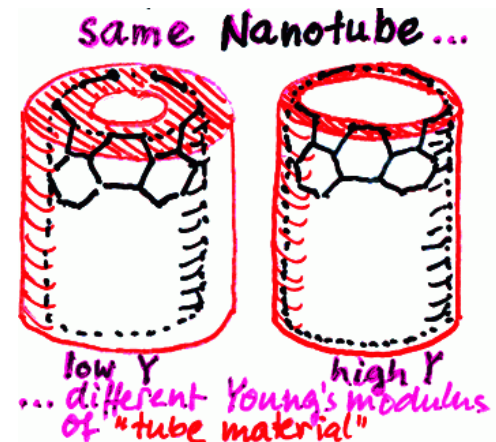
- **Observation:**

*[M.M.J. Treacy, T.W. Ebbesen, and J.M. Gibson, Exceptionally high Young's modulus observed for individual carbon nanotubes, Nature 381, 678 (1996)]*

**$Y \approx 4$  TPa**



“Young's modulus” of nanotubes



# Tough, light-weight nanotubes are crucial for the “2020” Space Elevator Concept



# Strain energy estimates

- Continuum elasticity theory ignores precise atomic positions



- Strain in deformed  $sp^2$  bonded graphene sheet is given by:
  - flexural rigidity:  $D=1.41$  eV
  - Poisson's ratio:  $\alpha=0.165$
  - (Reference System: Planar Graphene Sheet)

## Energy of fullerenes, nanotubes, scrolls

**Cylinder:**  $\Delta E_s = \pi D L / R = \varepsilon_{\text{cyl}} L / R$

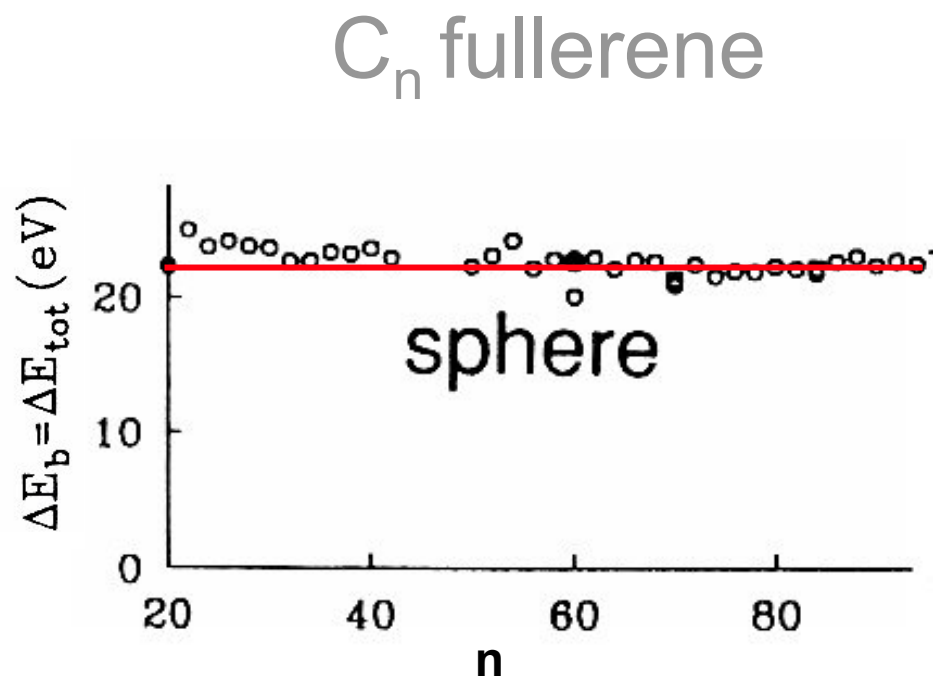
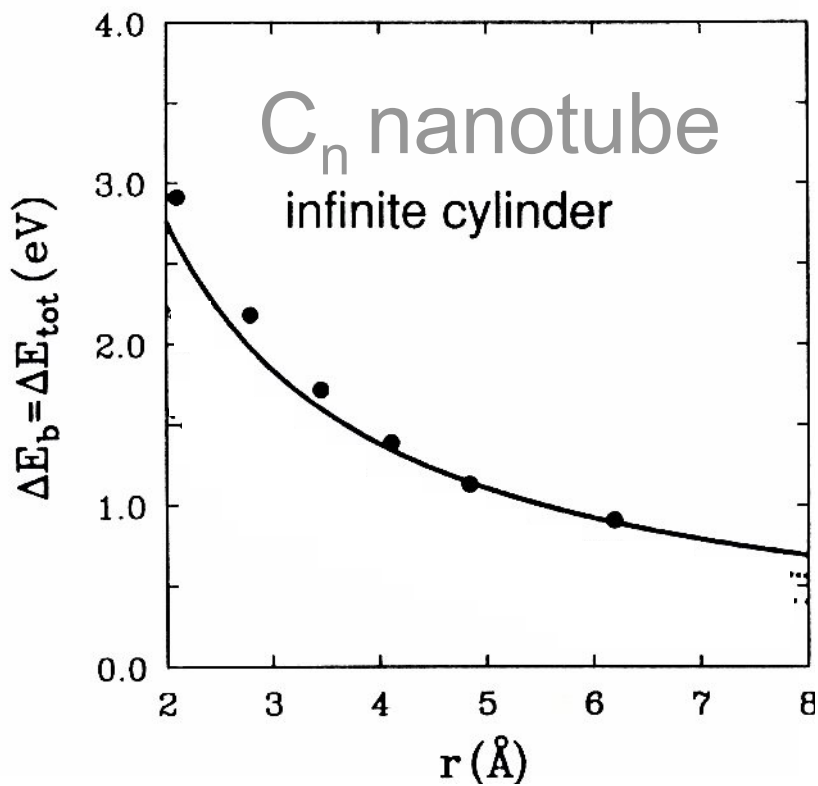
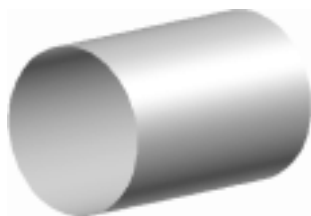
( $\varepsilon_{\text{cyl}} = 4.43 \text{ eV}$ ,  $R = \text{radius}$ ,  $L = \text{axial length}$ )



**Sphere:**  $\Delta E_s = 4\pi D(\alpha + 1) = 20.6 \text{ eV}$



## Reliability of the continuum description

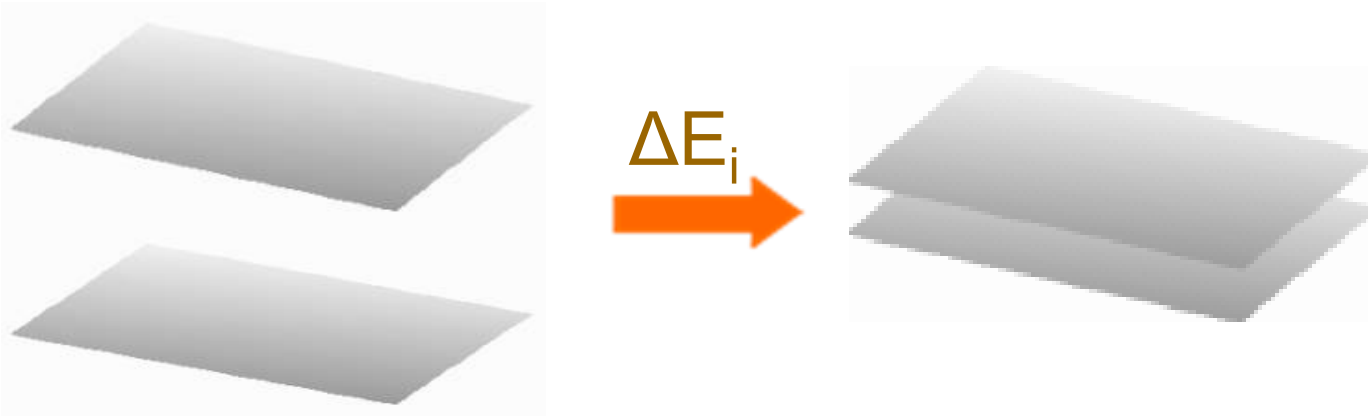




# Additional terms in finite-size and multi-wall systems

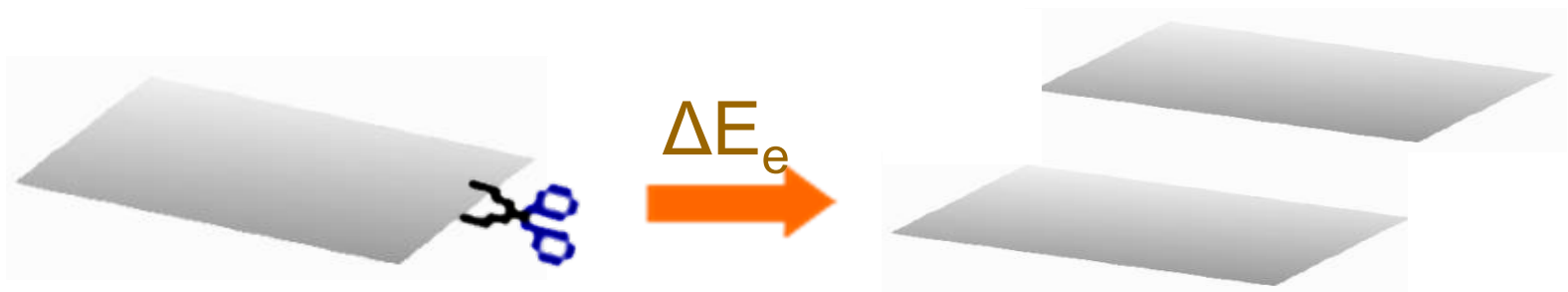
## Interlayer Interaction:

$$\Delta E_i = \varepsilon_{\text{vdw}} A \quad (\varepsilon_{\text{vdw}} = 2.48 \text{ eV/nm}^2, \quad A = \text{area})$$

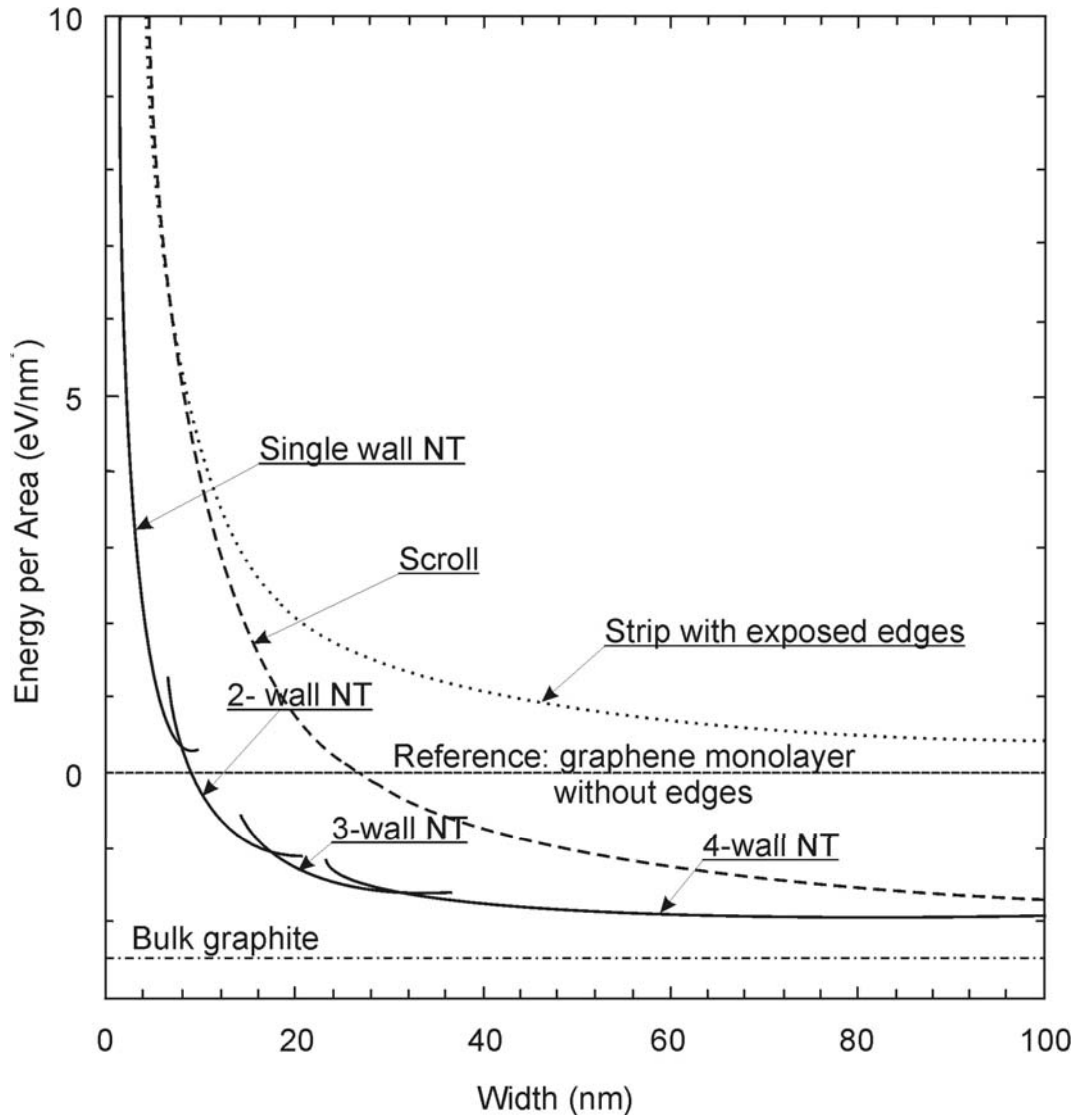


## Exposed Edge:

$$\Delta E_e = \varepsilon_e L \quad (\varepsilon_e = 21 \text{ eV/nm})$$



# Strain energy of scrolls and nanotubes



- Strain energy described by Continuum Elasticity Theory
- Energy corresponds to optimum geometry
- Multiwall nanotubes are always more stable than scrolls

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  - Graphitic  $sp^2$  versus diamond  $sp^3$  bonding
  - High Young's modulus
- **Chemical and thermal resilience, and thermal conductivity**
  - **Chemical resilience**
  - **Thermal stability**
  - **High thermal conductivity**
  - **Thermal contraction**
- Summary and Conclusions

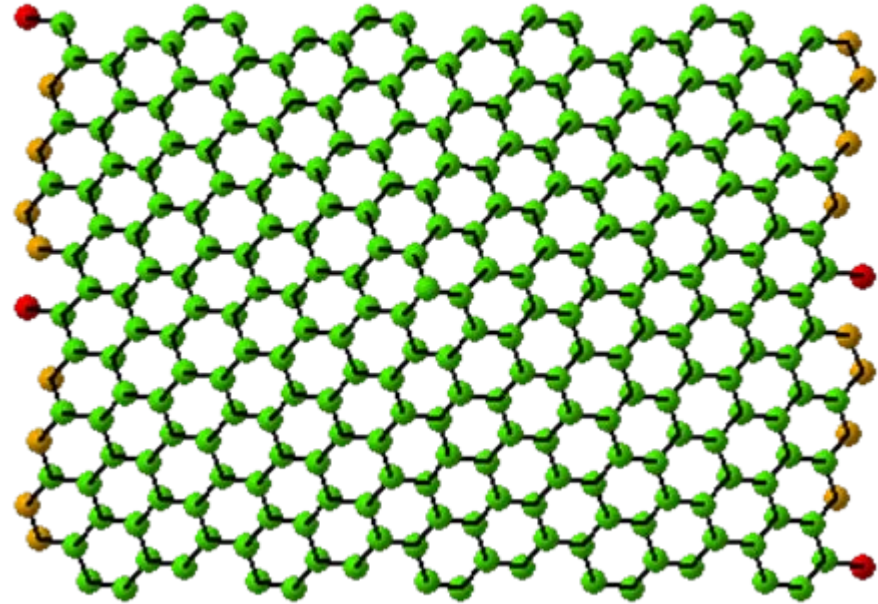
# Chemical and thermal resilience, and thermal conductivity

## Chemical resilience

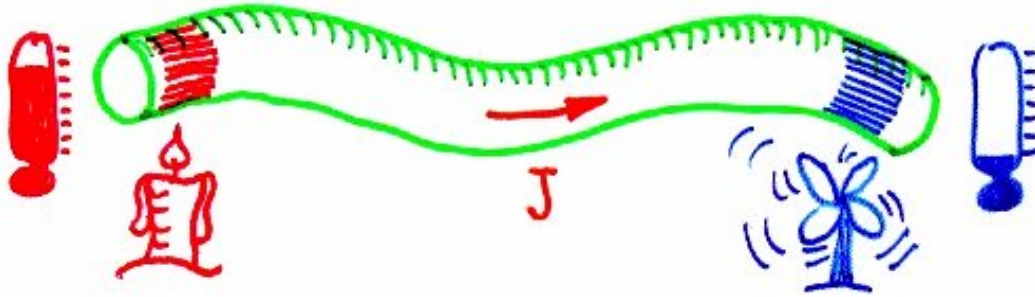
- Carbon nanotubes are chemically unreactive, similar to graphite

## Thermal stability

- Melting temperature of carbon nanotubes is similar to that of graphite,  $T_M \approx 4000 \text{ K}$

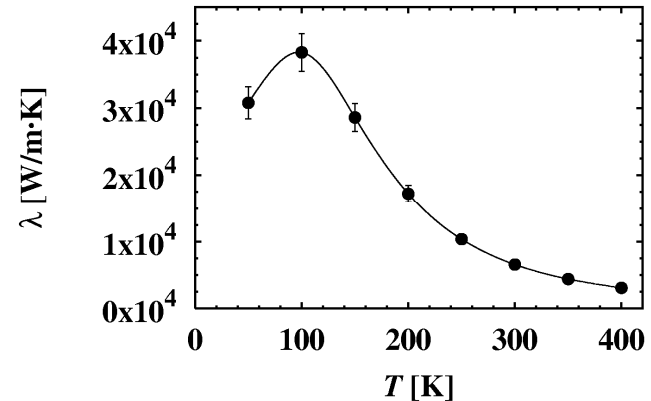


# High Thermal Conductivity



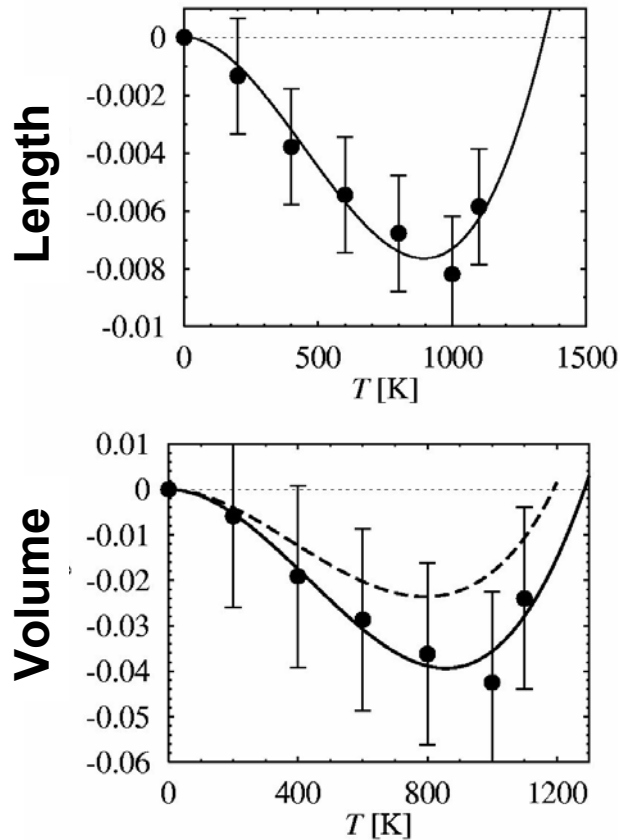
[Savas Berber, Young-Kyun Kwon, and David Tománek, *Phys. Rev. Lett.* 84, 4613 (2000)]

- NanoNanotubes may help solve the heat problem in nanoelectronics:
  - Efficient conductors of electrons and heat
  - Record Heat Conductivity:
    - Diamond (isotopically pure): 3320 W/m/K
    - Nanotubes: 6,600 W/m/K (theory, SWNT)  
>3,000 W/m/K (experiment, MWNT)
- Origin: combination of large phonon mean free path, speed of sound, hard optical phonon modes



Temperature dependence of the thermal conductivity  $\lambda$  for a (10,10) carbon nanotube for temperatures below 400 K

# Thermal contraction



Savas Berber,  
Young-Kyun Kwon,  
and David Tománek,  
*Phys. Rev. Lett.* **92**,  
015901 (2004)

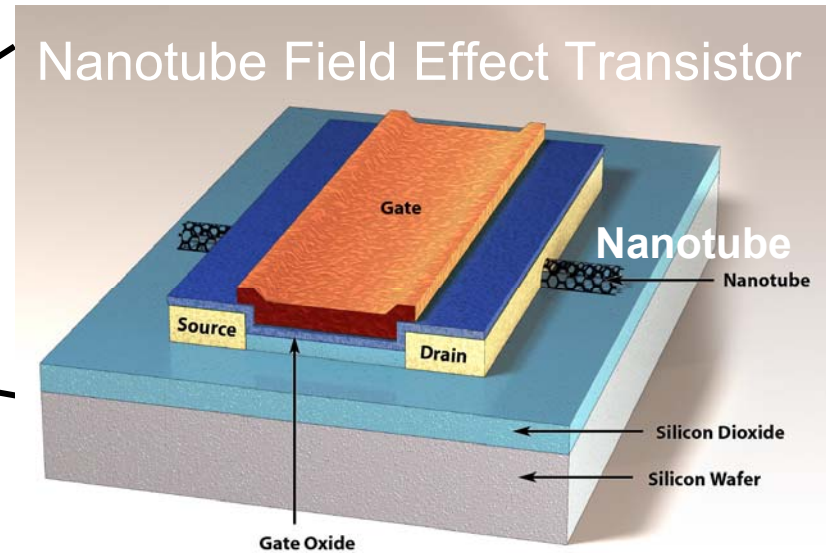
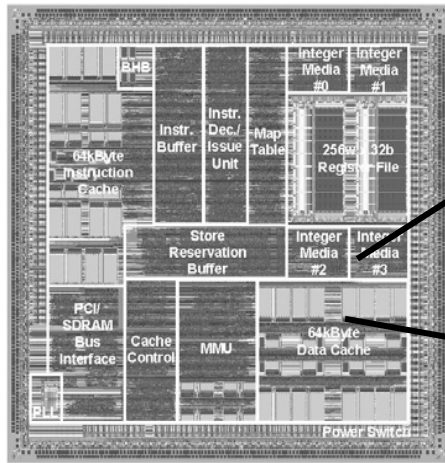
*See also Comment  
and Reply:*  
*Phys. Rev. Lett.* **94**,  
209702 (2005)

- ◆ Nanotubes contract rather than expand
- ◆ Physical origin: length contraction due to a gain in configurational and vibrational entropy

# Outline

- ....
- ....
- **Limitations of nanotube devices**
  - **How stable are defective tubes?**
  - **Deoxidation of defective nanotubes**
- Acknowledgments and the real end

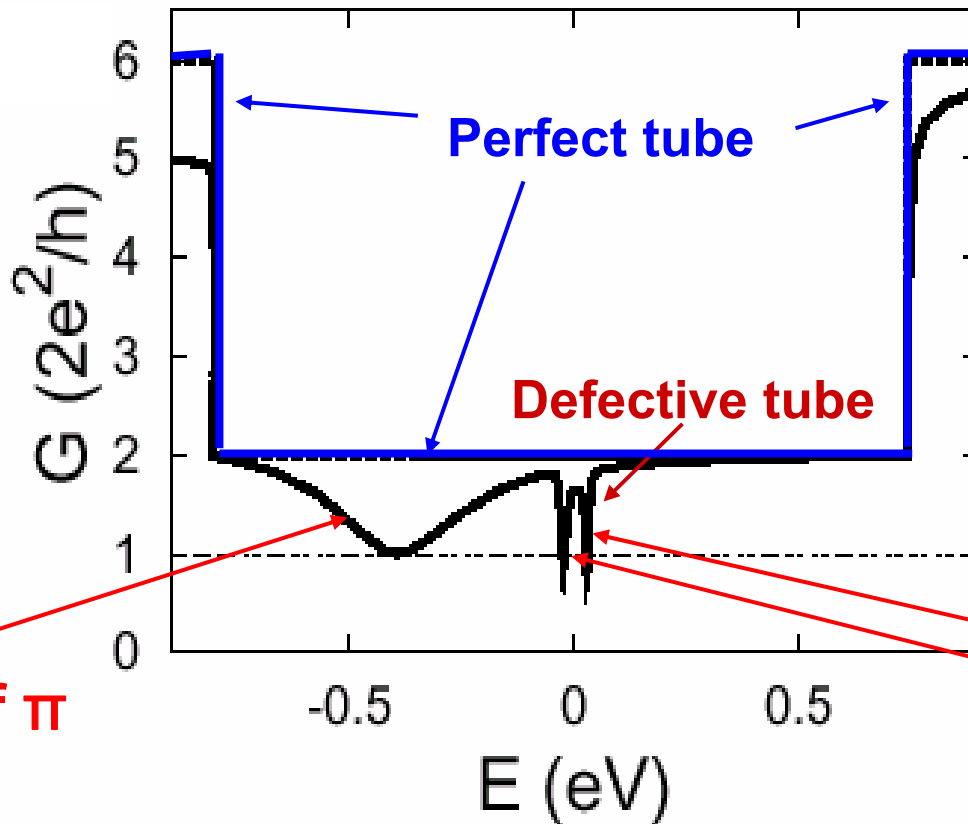
# Limitations of nanotube devices



- What **limits the speed** of nanotube-based electronics?
- How to **best contact** a carbon nanotube?
- How to **inter-connect** carbon nanostructures?
- Are nanotube devices as **sensitive to defects** as Si-LSI circuits?
- Can defects **heal themselves**?
- Are there ways to **selectively remove defects**?



# Quantum conductance of a (10,10) nanotube with a single vacancy



Choi, Ihm,  
Louie, Cohen,  
PRL (2000)

Missing  
network of  $\pi$   
electrons

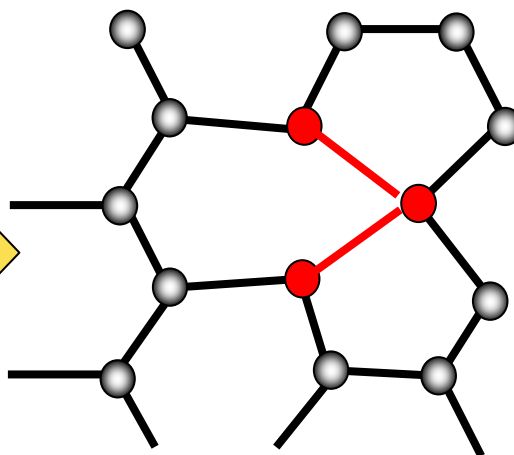
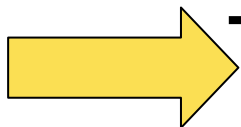
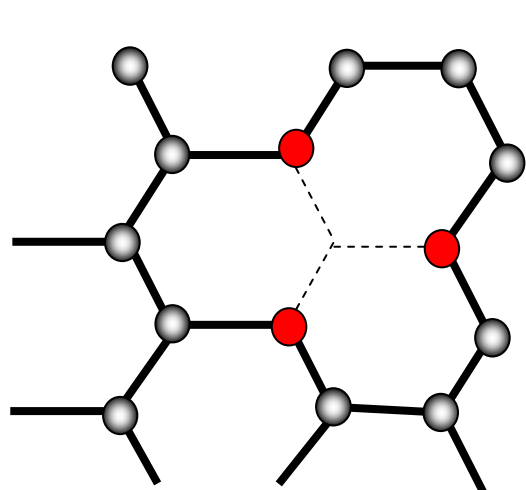
Dangling  
bonds:  $\sigma$   
electrons



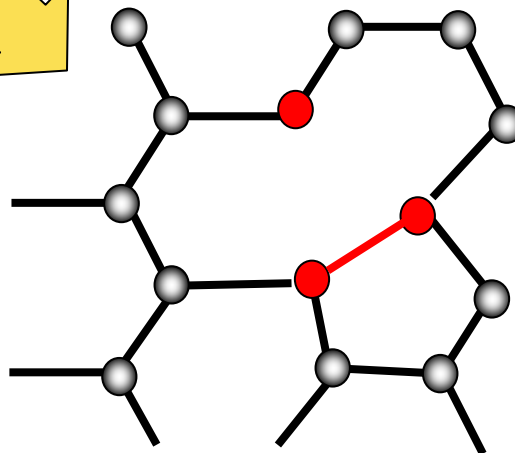
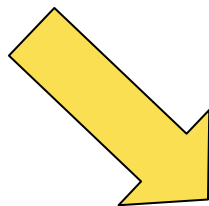
Individual defects significantly degrade  
conductance of a nanotube



# Equilibrium structure near a monovacancy in $sp^2$ carbon



Strain  
too large

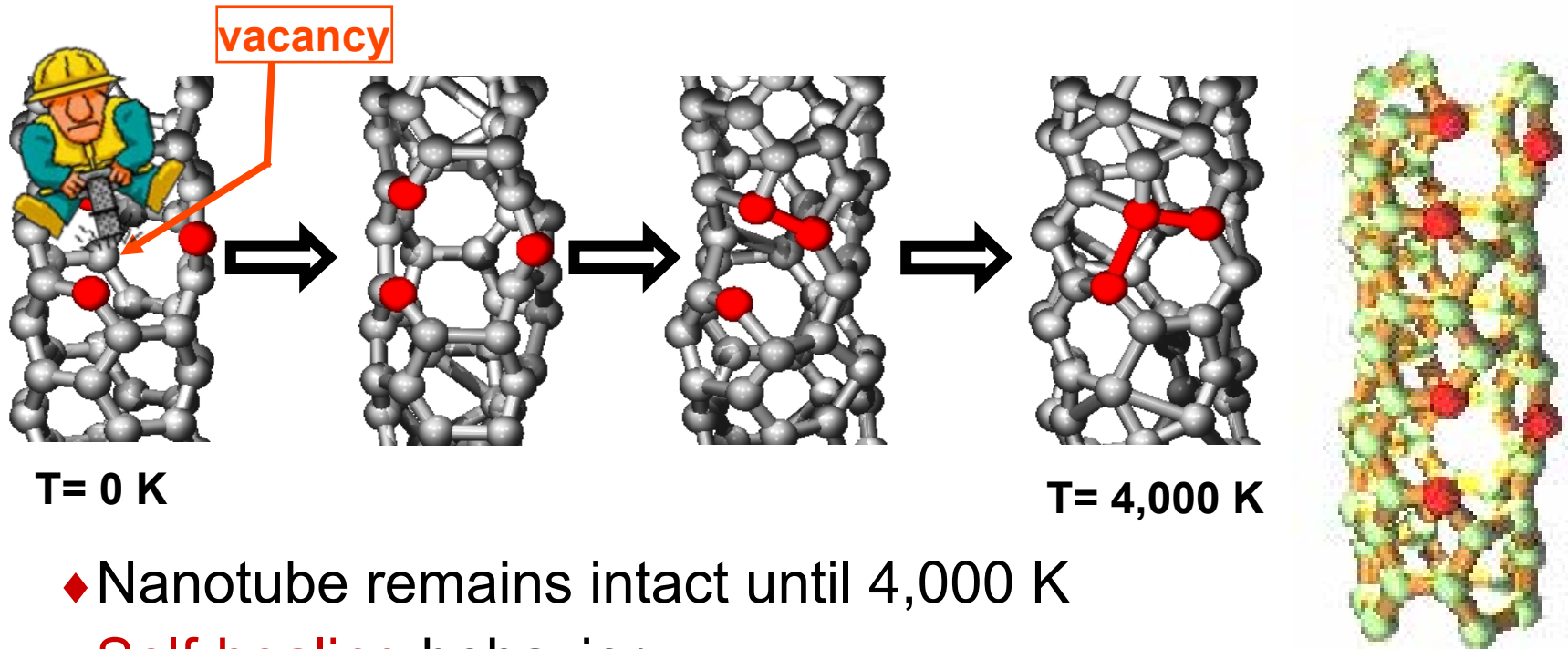


Barely stable

# How stable are defective tubes?

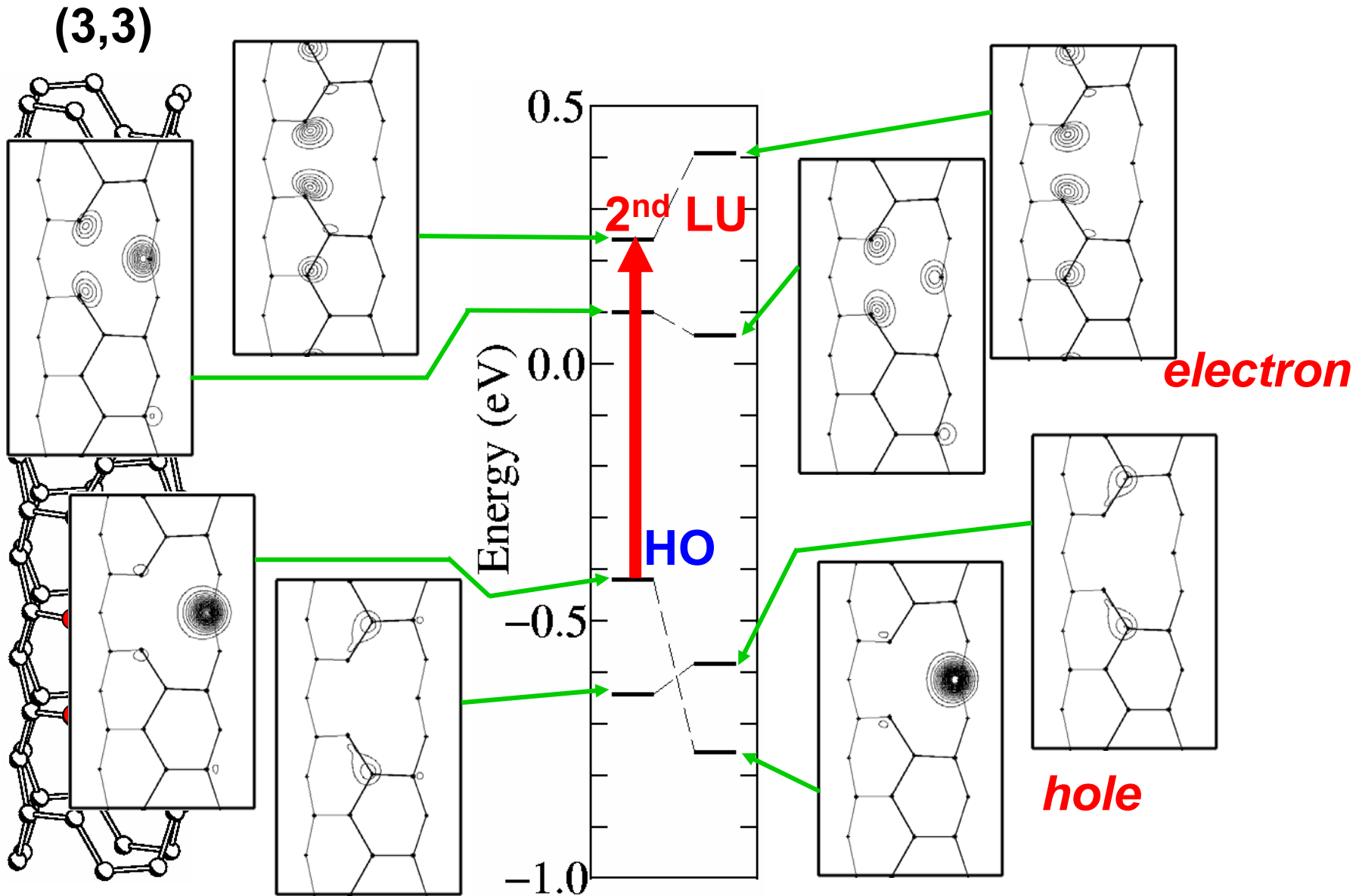
## Stability of defective tubes at high temperatures

- ◆ Danger of pre-melting near vacancies?

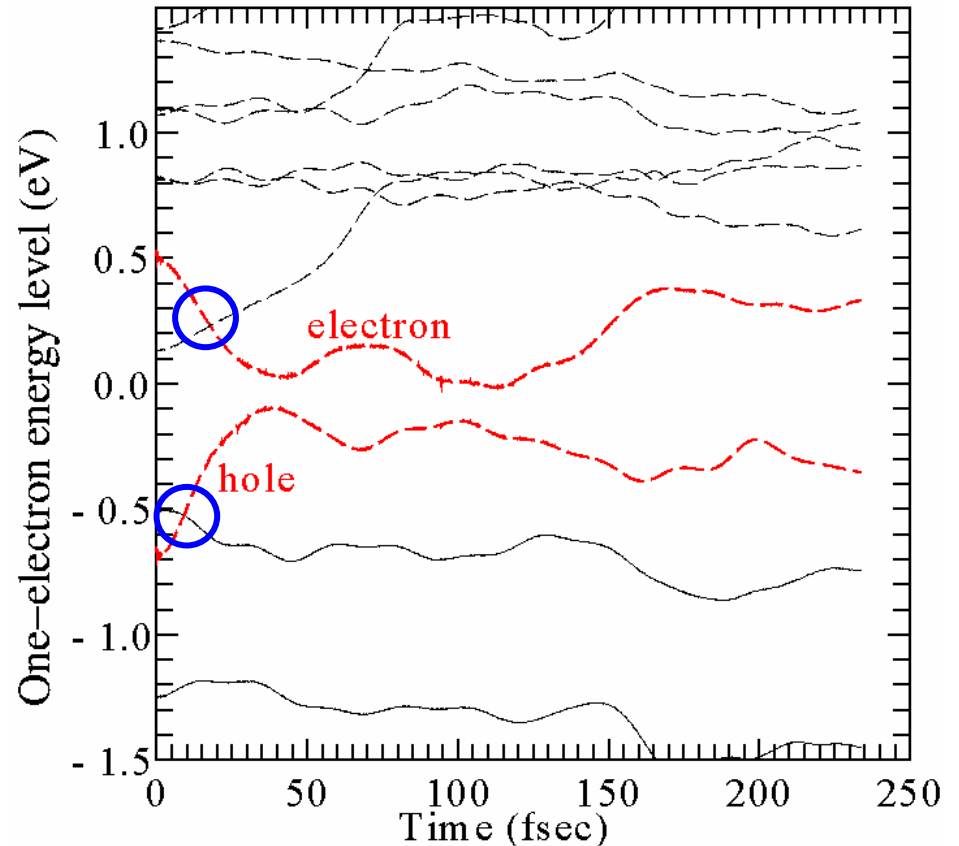
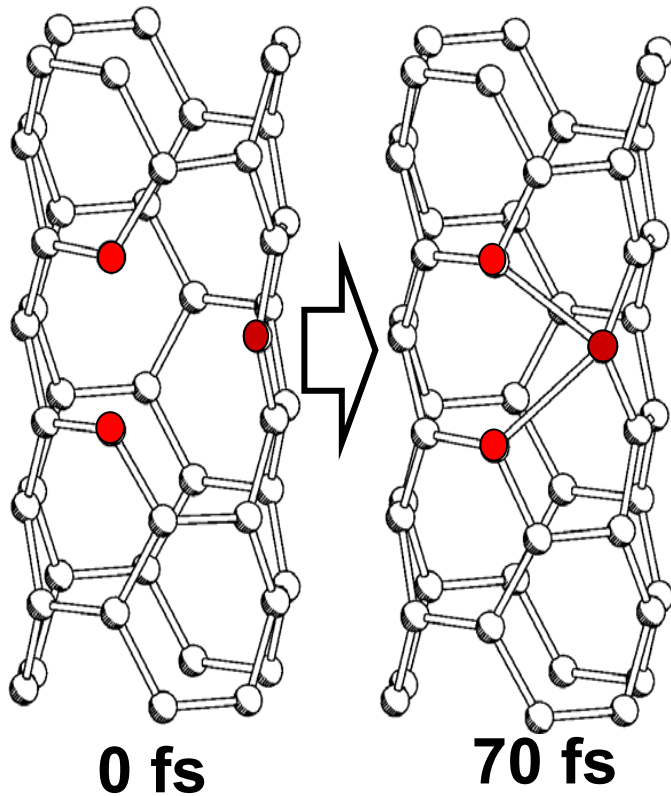


- ◆ Nanotube remains intact until 4,000 K
- ◆ **Self-healing** behavior:  
Formation of new bond helps recover
  - structural stiffness
  - conductance

# Optical excitation ( $\Delta E=0.9$ eV)



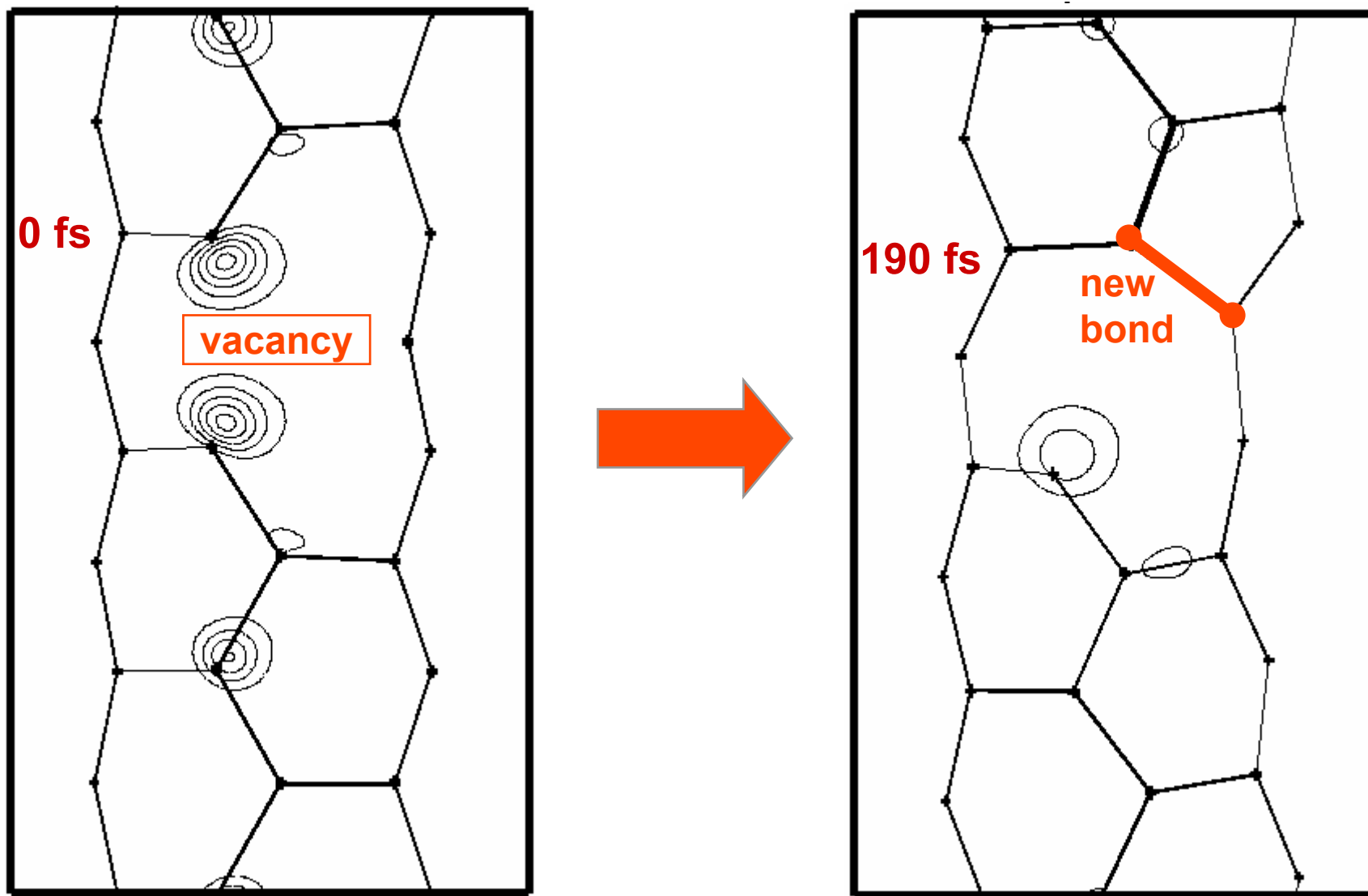
# Time evolution of the electronic states



$$\Psi_n(t+\Delta t) = \exp(-i/\hbar H\Delta t) \Psi_n(t)$$

- ◆ Very long-lived excitation
- ◆ Correct PES is followed in case of level alternation

# Structural changes under illumination

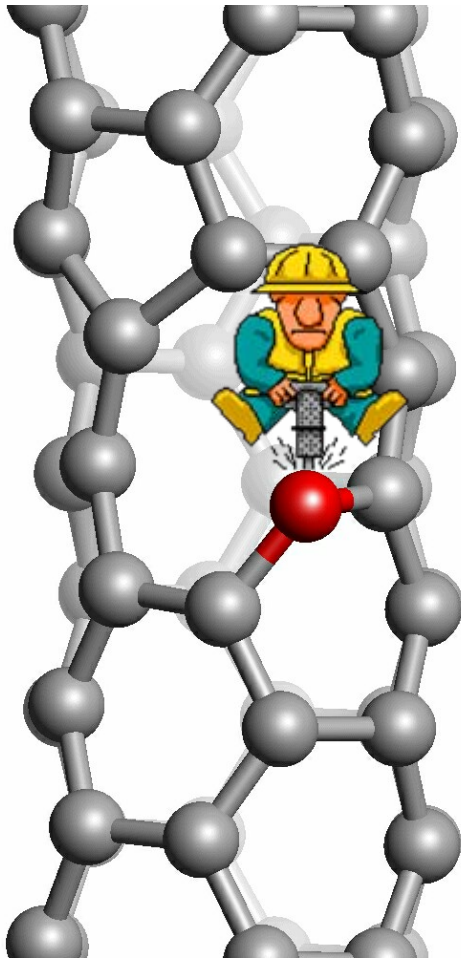


◆ **Self-healing** due to new bond formation

Y. Miyamoto, S. Berber, M. Yoon, A. Rubio, D. Tománek, Can Photo Excitations Heal Defects in Carbon Nanotubes? Chem. Phys. Lett. 392, 209–213 (2004)

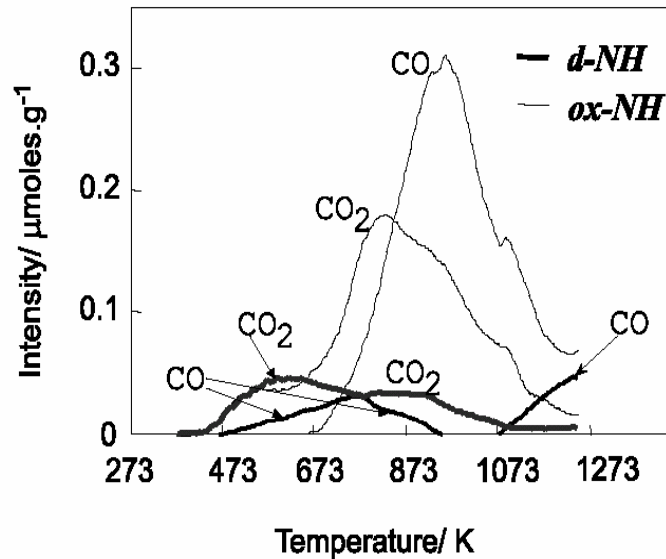
# Deoxidation of defective nanotubes

How to deoxidize?

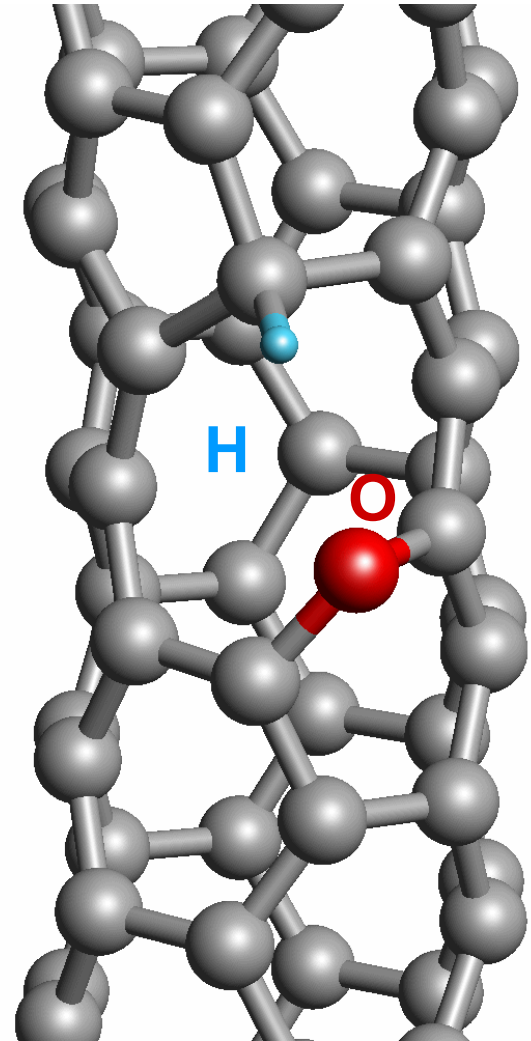


▪By heat treatment?

⇒No: Larger damage to nanotube



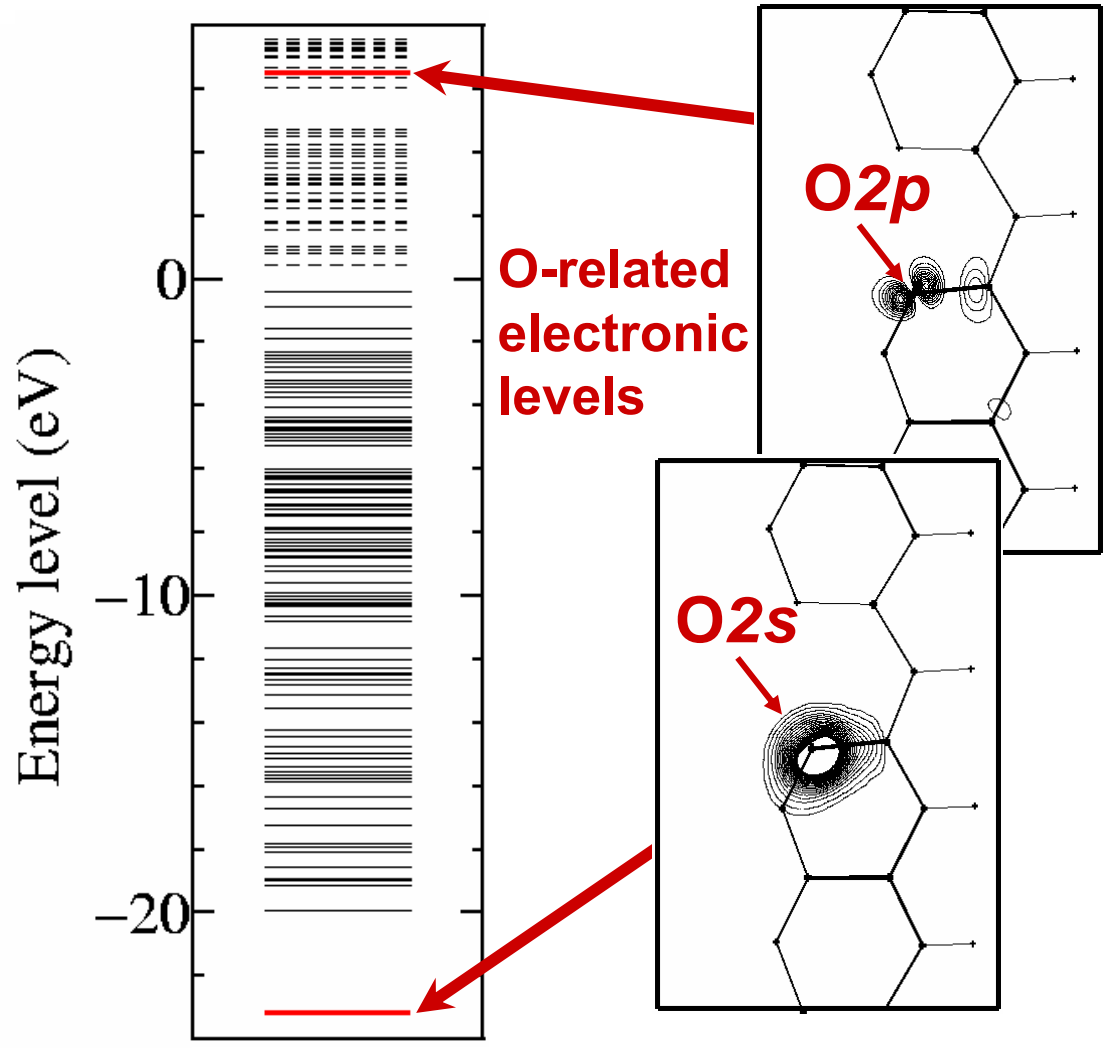
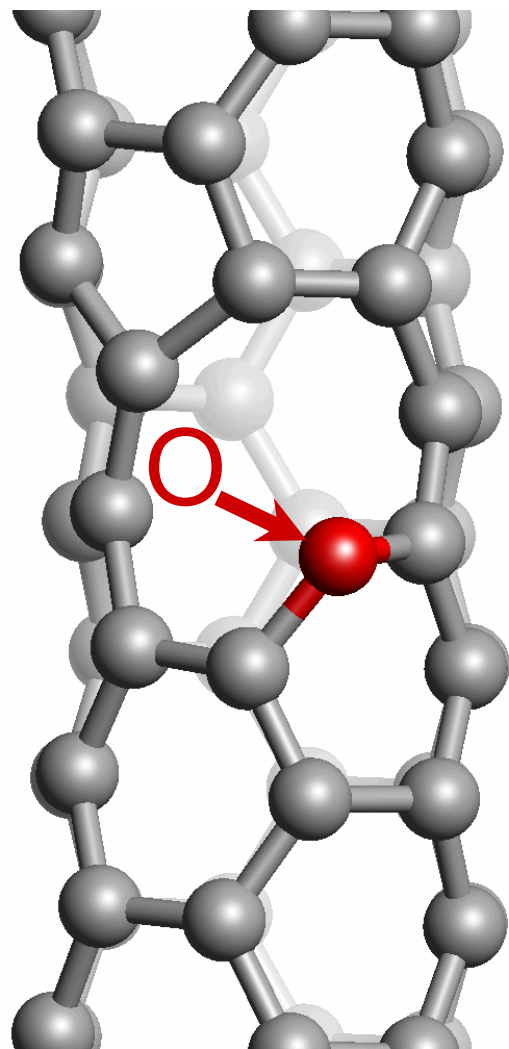
▪By chemical treatment with H?



Yoshiyuki Miyamoto, Noboru Jinbo, Hisashi Nakamura, Angel Rubio, and David Tománek, Photosurgical Deoxidation of Nanotubes, Phys. Rev. B 70, 233408 (2004).

Alternative to thermal and chemical treatment

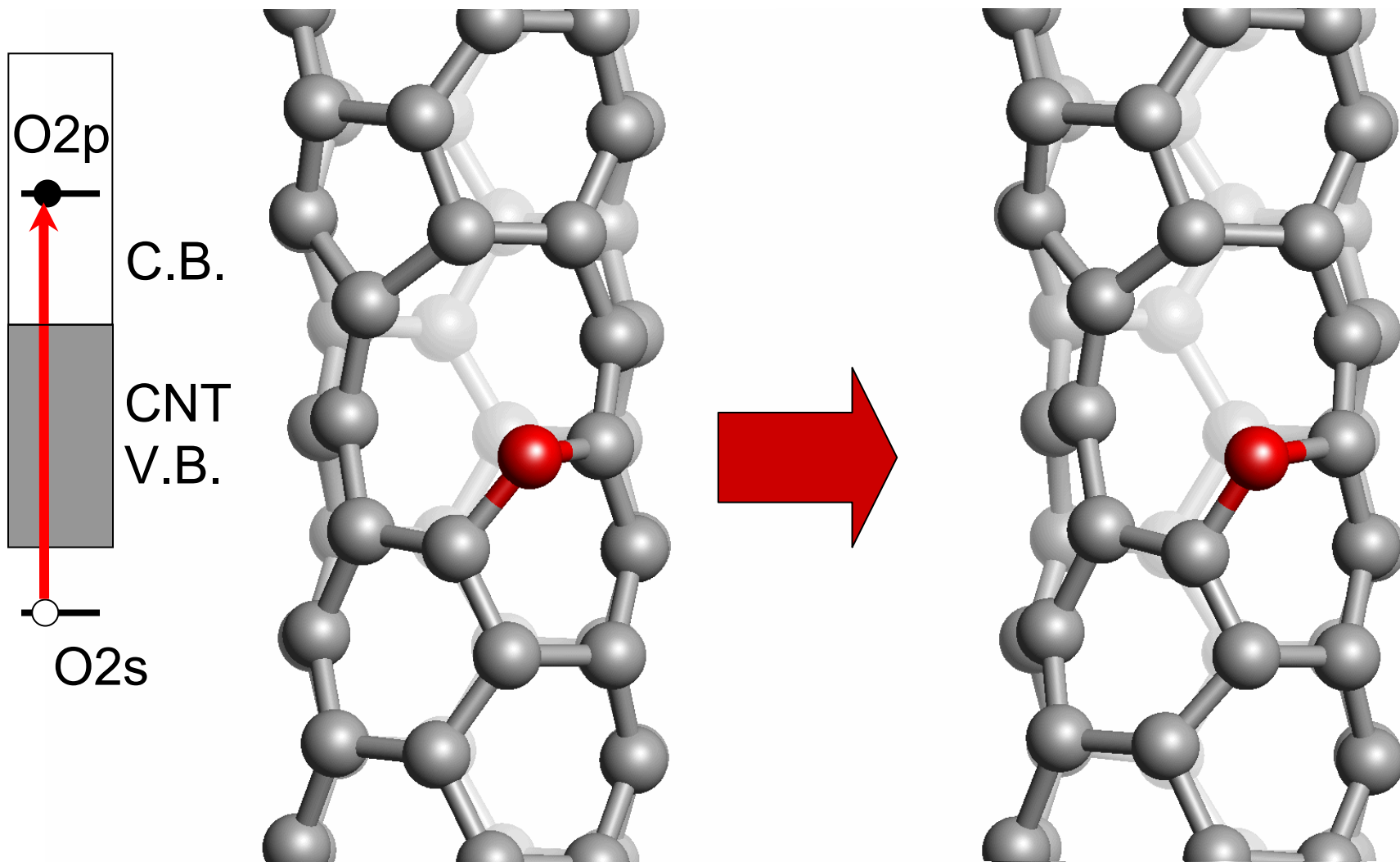
*Electronic excitations!*



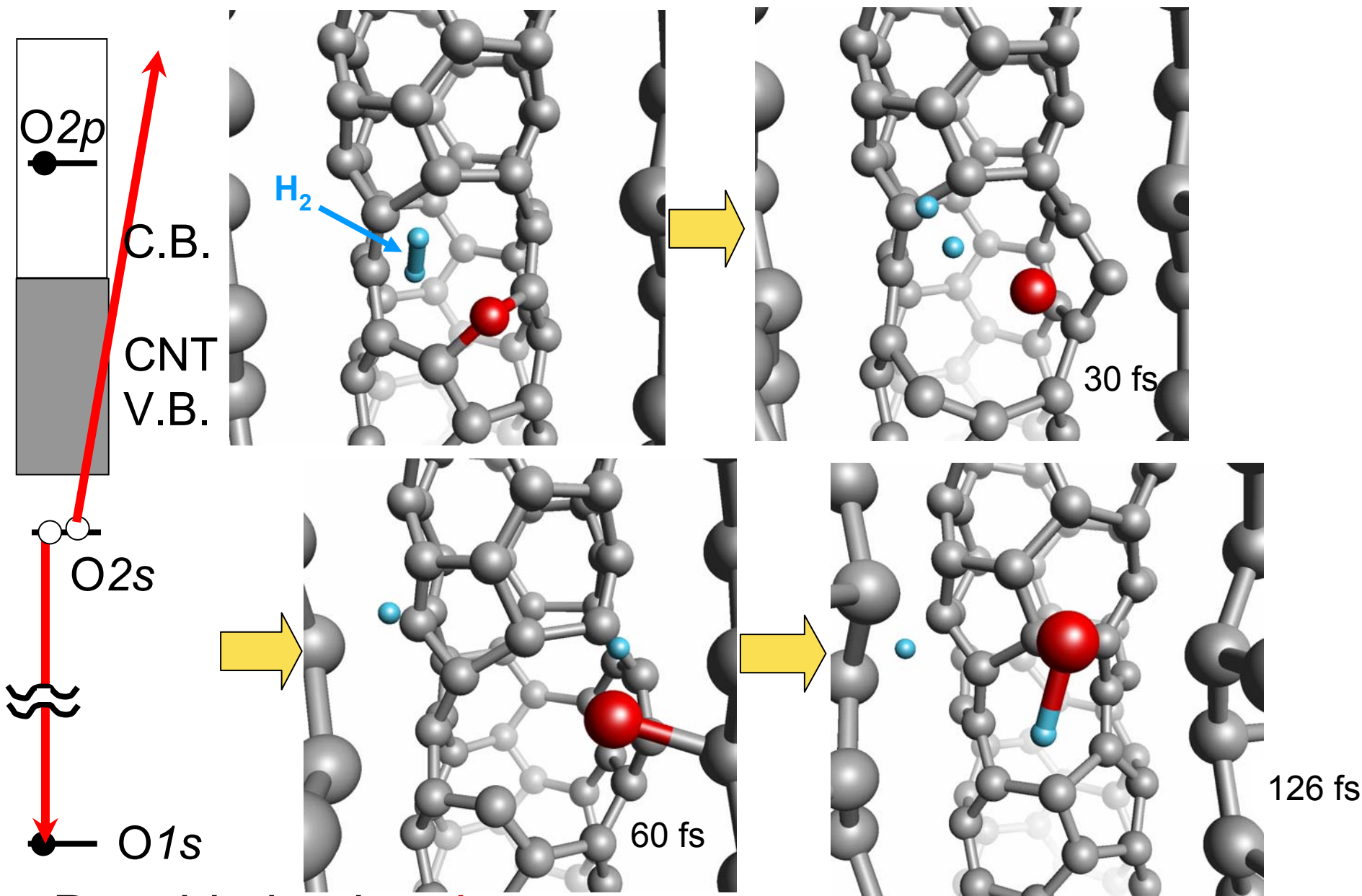


$O2s \rightarrow O2p$  excitation (33 eV)

hopeless



# Auger decay following the $O1s \rightarrow 2p$ excitation ( $\sim 520$ eV)



◆ Deoxidation by **photo-surgery**

# Acknowledgements

Savas Berber,	<i>University of Tsukuba, Japan</i>
Young-Kyun Kwon,	<i>University of Massachusetts, Lowell</i>
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Hisashi Nakamura,	<i>RIST Tokyo</i>
Angel Rubio,	<i>University of Pais Vasco, Spain</i>

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Jesper Nygård *University of Copenhagen*

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JAMSTEC-ESC (Japan)  
RIST (Japan)

